

1 **Constraining the pattern and magnitude of forced precipitation change in**  
2 **CMIP6**

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9 ABSTRACT: Projections of precipitation from global climate models are crucial for socioeco-  
10 nomic risk assessments under different emission scenarios, yet model discrepancies in the pattern  
11 and magnitude of future changes limit their application. Here, we show that using a pattern filter-  
12 ing technique can improve the accuracy with which the response of precipitation to anthropogenic  
13 forcing can be identified. Low-frequency component analysis is used to do so for four economically-  
14 relevant precipitation characteristics (mean intensity, wet day frequency, and extreme intensity and  
15 frequency) within individual CMIP-6 models. This approach improves agreement on the pattern  
16 of change by limiting the obscuring role of internal variability, but inherent model-biases remain  
17 considerable: 90% of models agree on the sign of change across 53, 36, 77, 66% of land area for  
18 each metric respectively. Despite these discrepancies in the sign of regional change, we find that  
19 differences in their average magnitude are well constrained by global surface warming ( $R^2$  of 0.9,  
20 0.89, 0.74, 0.77). Moreover, we show that these temperature-precipitation scaling relationships can  
21 be identified robustly within individual climate models from inter-temporal changes in the detected  
22 forced response (median  $R^2$  of 0.83, 0.77, 0.82, 0.93). Inter-model spread in these relationships  
23 is considerable (coefficient of variation of 20-40%) and the differences between models often  
24 significant, thus diagnosing a source of the uncertainty in the magnitude of projected precipitation  
25 change. These results suggest that despite uncertainty in the spatial pattern, the magnitude of  
26 future precipitation changes is well constrained by temperature-scaling relationships both across  
27 and within climate models. These relations may offer a potential avenue to constrain the magnitude  
28 of future projections, as well as complementary information for impact assessments.

## 29 **1. Introduction**

30 The hydrological cycle is likely to play a key role in the socio-economic impacts of future  
31 climate change. Key determinants of social welfare, such as agricultural productivity (Liang  
32 et al. (2017)), flood damages (Davenport et al. (2021); Willner et al. (2018b)) and social stability  
33 (Hsiang et al. (2013); von Uexkull et al. (2016)) are closely linked to changes in precipitation.  
34 Moreover, recent work has delineated specific aspects of the distribution of precipitation which  
35 impact macroeconomic production, including annual totals, wet day frequency as well as the  
36 intensity and frequency of daily extremes (Damania et al. (2020); Holtermann (2020); Kotz et al.  
37 (2022)). Understanding how these characteristics of precipitation will change under anthropogenic  
38 influence is therefore crucial for informing risk assessments and climate policy. Climate models  
39 such as those in the Coupled Model Intercomparison Project (CMIP6; Eyring et al. (2016)) play  
40 a crucial role in this understanding, providing projections of precipitation under different levels of  
41 greenhouse forcing at the regional and temporal detail necessary for assessment of these impacts  
42 (Warszawski et al. (2014)). These projections can subsequently inform detailed assessments of the  
43 consequences of both mitigation (Lange et al. (2020); Thiery et al. (2021)) and adaptation (Willner  
44 et al. (2018a); Boulange et al. (2021)).

45 Despite recent progress, large uncertainties exist in projections of future precipitation change  
46 (Knutti and Sedláček (2013); Shepherd (2014)) which limit their utility in informing these impact  
47 assessments. From a global perspective, changes in average precipitation rates are constrained  
48 by the atmospheric energy budget to increase at a rate of  $2\text{-}3\%K^{-1}$  (Allen and Ingram (2002)).  
49 However, at the regional level the role of atmospheric circulation is important and complex, and  
50 changes in regional averages are less certain. Although particular components of circulation  
51 change, such as the weakening of the tropical Pacific circulation, are understood physically and  
52 have been detected clearly in models and historical observations (Held and Soden (2006); Vecchi  
53 and Soden (2007); Vecchi et al. (2006)), the resulting changes in precipitation can still be difficult to  
54 constrain because minor differences in the extent of shifting circulation can imply large differences  
55 in even the sign of regional precipitation change (Chadwick et al. (2016)). Consequently, dynamical  
56 changes from circulation remain a large source of the considerable uncertainty in projections of  
57 average regional precipitation (Chadwick et al. (2013); Ma and Xie (2013); Kent et al. (2015);  
58 Long et al. (2016); Shepherd (2014); Fereday et al. (2018)).

59 By contrast, changes in daily precipitation extremes are predominantly determined by thermody-  
60 namic effects relating atmospheric water vapour content to temperature (Allen and Ingram (2002);  
61 Fischer and Knutti (2016)). This thermodynamic contribution is simpler and hence more con-  
62 sistent projected across models (Pfahl et al. (2017)). Moreover, its dominance over circulation  
63 changes means that precipitation extremes have undergone a near-global increase which is well  
64 documented in historical observations (Min et al. (2011); Zhang et al. (2013); Fischer and Knutti  
65 (2016); Chen and Sun (2017); Kirchmeier-Young and Zhang (2020); Madakumbura et al. (2021)).  
66 Dynamical changes from atmospheric circulation cause only regional differences in the magnitude  
67 of these increases which constitute the majority of the projected uncertainty between models (Pfahl  
68 et al. (2017)).

69 To aid our understanding and application of precipitation projections, we here aim to explore their  
70 discrepancies in terms of both the spatial pattern and the magnitude of future regional changes. To  
71 maximise the applicability of our results for impact assessments, we focus on the changes over land  
72 of four key aspects of the distribution of precipitation from which impacts on economic production  
73 have been identified (Kotz et al. (2022)), namely: mean precipitation rates, wet day frequency and  
74 the intensity and frequency of daily extremes. We apply a pattern filtering technique (Wills et al.  
75 (2018, 2020)) to separate the forced response to anthropogenic influence from internal variability  
76 separately within each member of a multi-model CMIP-6 ensemble. This approach accounts for  
77 spatio-temporal correlations while detecting the forced response, aiming to limit the obscuring  
78 role of internal variability and hence improve our assessment of inter-model discrepancies. This  
79 is of particular importance given the relatively strong internal variability present in precipitation  
80 characteristics (Deser et al. (2014)).

81 Our approach improves agreement between models on the spatial pattern of the forced response,  
82 but inherent model discrepancies remain considerable, in particular for mean precipitation and wet  
83 day frequency. However, we find that the magnitudes of regional change are very well constrained  
84 by the extent of global mean temperature (GMT) change. Interestingly, these relationships are  
85 improved when the absolute value of regional precipitation change is assessed, considerably so for  
86 mean precipitation and wet day frequency. This suggests that although models may disagree on  
87 the sign of regional change, particularly for precipitation characteristics which are dominated by  
88 uncertain circulation changes, the magnitude of such change is well constrained by the underlying

89 thermodynamic forcing of the climate system i.e. GMT changes. We further demonstrate that  
 90 these temperature-precipitation scaling relations are robustly identifiable within individual climate  
 91 models from inter-temporal changes in the detected forced response. The rates at which precip-  
 92 itation changes scale with GMT show considerable and significant differences between models,  
 93 thus diagnosing a source of the uncertainty in the magnitude of projected precipitation change, and  
 94 offering a potential avenue to constrain them.

## 95 **2. Data and Methods**

### 96 *a. CMIP6 data*

97 We use daily surface precipitation rates and daily 2-m temperature from 21 climate models  
 98 participating in CMIP6. We choose models which provide output under both the historical (1850-  
 99 2014) and the future (2015-2100) greenhouse forcing scenarios specified by SSP126 and SSP585.  
 100 A full list of models is displayed in Figs. A1-4.

### 101 *b. Precipitation indices*

102 Our assessment of precipitation change focuses on a number of key characteristics of the dis-  
 103 tribution of daily precipitation which have been demonstrated to have significant impacts on  
 104 macroeconomic production (Kotz et al. (2022)). Therefore, the following four annual precipitation  
 105 indices are calculated from daily precipitation rates on the native grids of each CMIP6 model over  
 106 land: the annual mean precipitation rate (calculated over all days),

$$Pm_{x,y} = \frac{1}{N_y} \sum_{d=1}^{N_y} P_{x,d} \quad (1)$$

107 the annual frequency of wet days (defined using a 1mm threshold),

$$Pw d_{x,y} = \sum_{d=1}^{N_y} H(P_{x,d} > 1mm) \quad (2)$$

108 the annual daily maximum as a measure of the intensity of daily extremes,

$$PX1_{x,y} = \max(P_{x,d} : x = 1, \dots, N_y) \quad (3)$$

109 and the annual number of days exceeding the 99<sup>th</sup> percentile of the historical distribution, 99p,  
110 (historical percentiles calculated over all days from 1850-1950) as a measure of the frequency of  
111 daily extremes,

$$P > 99p_{x,y} = \sum_{d=1}^{N_y} H(P_{x,d} > 99p) \quad (4)$$

112 where  $N_y$  is the number of days in a given year and  $H$  is the Heaviside step function, and  $x$  and  
113  $d$  respectively denote grid-cell and day. These annual measures are estimated on the native CMIP  
114 grids, before being linearly interpolated to a common 1-by-1 degree grid for further analysis.

### 115 *c. Separating the forced response from internal variability: low-frequency component analysis*

116 Identifying the forced response of the climate system to anthropogenic influence is complicated  
117 by natural internal variability (Deser et al. (2012)), particularly on the multi-decadal time-scales  
118 over which averages are often used to characterise a forced response (Masson-Delmotte et al.  
119 (2021)). One approach to overcome this issue is to use large ensembles of a single climate  
120 model in which internal variability can be characterised and removed by initialising ensemble  
121 members from different initial conditions (Kay et al. (2015)). However, to consider the full range  
122 of structural differences between models which can bias the forced response, a variety of climate  
123 models must be assessed. We do so using the multi-model ensemble CMIP6, and instead apply a  
124 pattern filtering technique to individual ensemble members to separate the forced response from  
125 internal variability. Low-frequency component analysis (LFCA) takes advantage of the different  
126 time-scales of the respective processes to identify the forced response from a single realisation with  
127 accuracy comparable to ensembles with up to 20 realisations (Wills et al. (2020)). We use LFCA  
128 over other methods, such as signal-to-noise maximising pattern-filtering, because of its superior  
129 performance in detecting the forced response from a single realisation (Wills et al. (2020)).

130 Here we provide a conceptual summary of LFCA and of its application to identifying the climatic  
131 response to anthropogenic forcing, please see Wills et al. (2018) for a more detailed introduction  
132 to and description of the method. LFCA is a form of linear-discriminant analysis which identifies  
133 independent modes which can account for the greatest ratio of low-frequency to total variance.  
134 Given the longer time-scales over which changes due to greenhouse forcing evolve in comparison

135 to those due to internal variability, this form of variance maximisation can accurately separate the  
136 two (Wills et al. (2018, 2020); Kotz et al. (2021)).

137 Linear recombinations of the leading empirical-orthogonal-functions, (EOFs) are found which  
138 maximise this variance ratio. We retain a sufficient number of EOFs to account for a minimum of  
139 70% of the original spatio-temporal variance, and define low-frequency variance as that resulting  
140 from applying a 20-year low-pass Butterworth filter with reflecting boundary conditions to grid-cell  
141 level departures from linear trends. We use a lower cut-off frequency than Wills et al. (2018, 2020),  
142 due to the lower signal-to-noise ratio of the climate change signal in precipitation than temperature  
143 (Deser et al. (2014)), but recover consistent results under alternative filtering specifications. The  
144 resulting linear recombinations are independent, and ordered in terms of increasing frequency.  
145 They constitute both a "low-frequency component" (LFC) and "low-frequency pattern" (LFP);  
146 the LFC is a time-series which describes the temporal evolution of the specific spatial pattern  
147 encompassed by the LFP. Given the longer time-scales over which anthropogenic forcing evolves  
148 compared to internal variability, we interpret the lowest-frequency component as the response to  
149 anthropogenic forcing, following Wills et al. (2020) and Kotz et al. (2021).

150 We apply LFCA to the four precipitation indices (over land areas) and to annual mean temperature  
151 (over the globe) from 1950-2100 under the anthropogenic forcing of the historical period and both  
152 the SSP126 and SSP585 future scenarios, having first linearly interpolated each index to a common  
153 1-by-1 degree grid. The forced change between two given time periods (usually between two  
154 decades) is then calculated as the product of the lowest-frequency LFP and the difference between  
155 temporal (usually decadal) averages of the corresponding LFC.

156 In a number of cases, we also estimate the forced changes in each precipitation metric using  
157 temporal averages of the data prior to any detection with LFCA. In these cases we either use 10  
158 (Fig. 2 and B6-B9) or 30 year periods (Fig. 2) to estimate the change.

#### 159 *d. Scaling between the magnitude of precipitation changes and temperature change*

160 To estimate the average magnitude of regional precipitation change, continental, area-weighted  
161 averages of the absolute regional change are calculated from the forced patterns of precipitation  
162 change identified with LFCA. For the extreme metrics, the regional changes are assessed in terms  
163 of percentage change from the historical (1850-1950) baseline in order to make comparison to

164 the theoretical expectations of the Clausius-Clapeyron relation. These land-area averaged absolute  
165 precipitation changes are then compared to estimates of the change in global mean temperature,  
166 calculated from the global-area average change in 2-m surface temperature estimated from the  
167 lowest-frequency component identified comparably with LFCA. In Fig. 4, changes in precipitation  
168 and temperature between 1950-1960 and 2090-2100 are compared between models. In Fig. 5  
169 changes between pairs of non-overlapping decades separated by 25-years within each individual  
170 model are used.

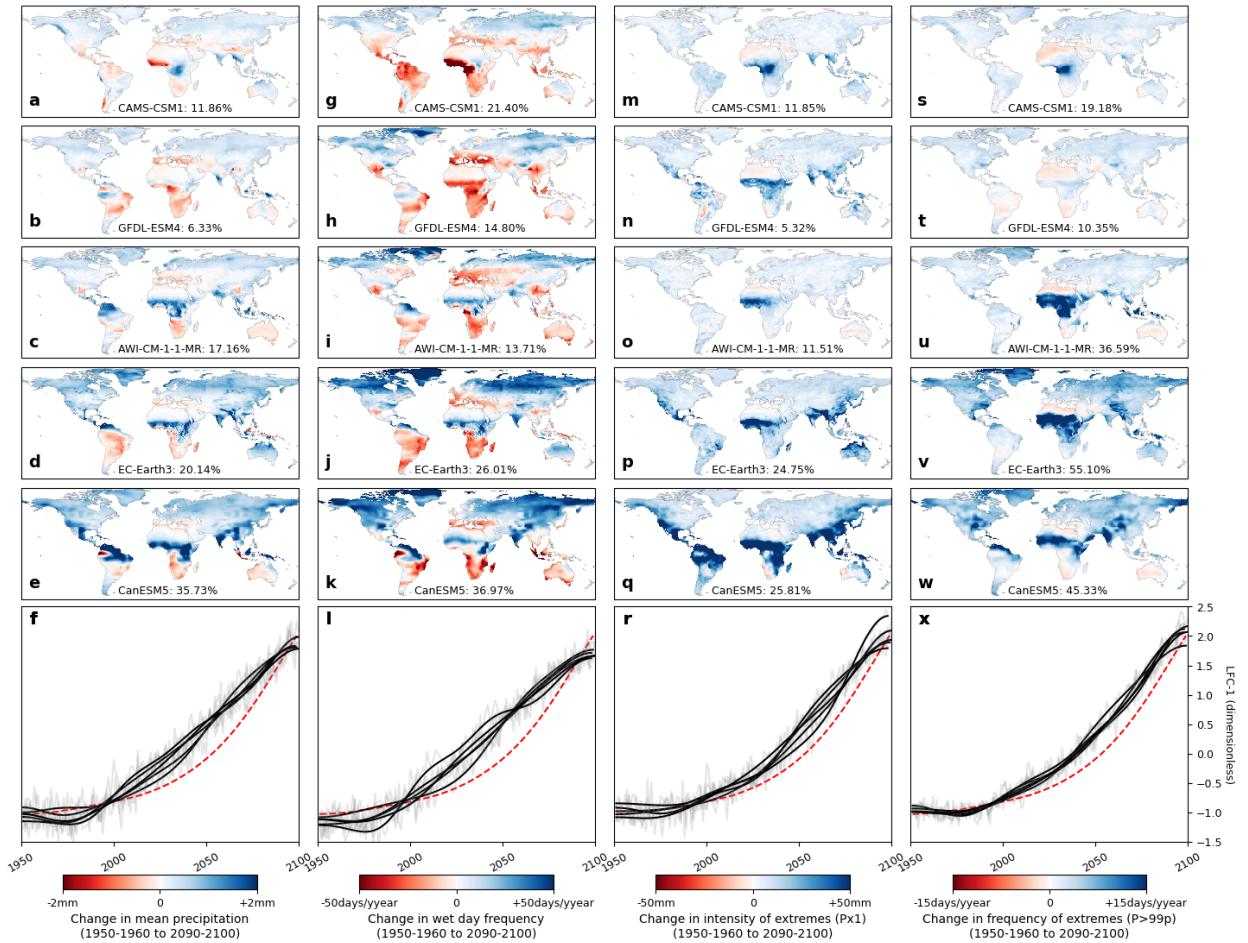
171 Linear scaling rates are estimated with a least-squares linear regression for mean precipitation  
172 and the number of wet days. Due to the theoretical expectations of the Clausius-Clapeyron  
173 relation for the extreme metrics, in these cases an exponential scaling is estimated by transforming  
174 the percentage precipitation changes,  $\frac{\delta P}{P}$ , into a logarithmic form,  $\log(\frac{\delta P}{P} + 1)$ . Methodological  
175 uncertainty in the estimates of these scaling rates is obtained via a bootstrapping approach. In  
176 Fig. 4, the selection of climate models is re-sampled 1000 times with replacement, whereas in  
177 Fig. 5 the different time periods are re-sampled equivalently. As such, these estimates reflect the  
178 methodological uncertainty arising from the available variety of climate models (in Fig. 4) and the  
179 variety of forcing occurring over the different periods of the available scenarios (in Fig. 5). When  
180 estimating the significance of differences between model scaling rates, we estimate a distribution  
181 of differences between model scaling rates from the 1000 re-sampled estimates, and assess whether  
182 the 95% confidence intervals of this distribution of differences encase zero.

### 183 **3. Results**

#### 184 *a. Detection of the precipitation response to anthropogenic-forcing in individual climate models*

185 We identify the response of mean daily precipitation, wet day frequency and the intensity and  
186 frequency of daily extremes to anthropogenic forcing (historical and SSP585) within individual  
187 CMIP6 climate models using LFCA. Fig. 1 shows results for a selection of five models (see Figs.  
188 A1-4 and A5-8 for results from all members of the ensemble under SSP585 and SSP126 forcing  
189 respectively). For each precipitation index and for each model, the lowest-frequency component  
190 (LFC-1) exhibits a near-monotonic trend which closely follows the increasing concentrations  
191 of greenhouse gases in the historical and SSP585 scenario. However, both the intensity and  
192 spatial pattern of the detected end-of-century forced change (1950-60 to 2090-2100) show clearer

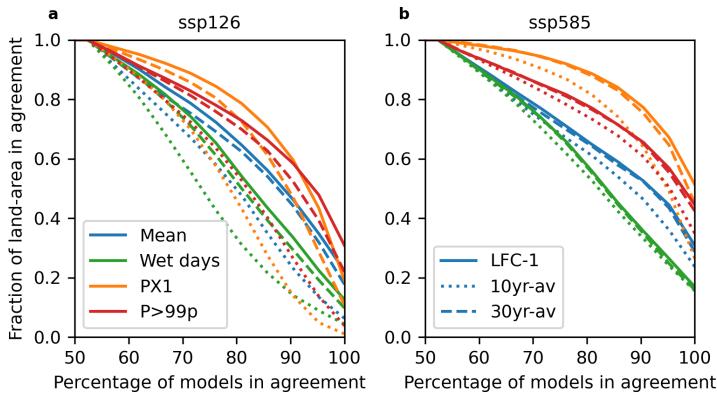
<sup>193</sup> differences between models. Maps of the forced-change are displayed separately for each model  
<sup>194</sup> to present the heterogeneity of modelling bias (see Figs. A1-4 for results from all models).



195 FIG. 1. The forced response of four precipitation characteristics to historical (1950-2014) and future (SSP585,  
 196 2015-2100) anthropogenic forcing, detected in individual CMIP6 climate models with low-frequency component  
 197 analysis. (a-e) The spatial pattern of the forced change in mean precipitation from 1950-60 to 2090-2100 (the  
 198 product of the lowest-frequency pattern with the difference between decadal averages of its corresponding  
 199 component) for a selection of models (see Fig. S1 for all 21 members of the CMIP-6 ensemble). (f) The  
 200 temporal evolution of the lowest-frequency components (LFC-1) of mean precipitation change are shown in grey  
 201 with a 20-year Butterworth filtered time-series in black. Time series for each model are overlain due to their  
 202 similarity. The concentration of greenhouse gases in the historical and SSP585 are rescaled and shown in red for  
 203 comparison. Corresponding results for changes in wet day frequency (g-l), the intensity of daily extremes (m-r)  
 204 and the frequency of daily extremes (s-x) are shown alongside. Models are ordered top to bottom in terms of their  
 205 respective GMT change. The model name is indicated in the bottom of each panel, along with the percentage of  
 206 total spatio-temporal variance accounted for by LFC-1.

207 *b. The spatial patterns of forced change - intermodel uncertainty*

208 We explore the extent of these biases in the modelled response of precipitation to anthropogenic  
209 forcing in Fig. 2, which shows the fraction of land area on which at least a certain proportion  
210 of models agree on the sign of forced change. Agreement is larger for the extreme metrics than  
211 for mean precipitation and the frequency of wet days, consistent with our expectations given the  
212 large contribution of uncertainty in the circulation response to discrepancies in changes in mean  
213 conditions (Shepherd (2014); Chadwick et al. (2016)). Agreement is also larger in the detected  
214 response to SSP585 forcing compared to SSP126, reflecting the fact that the stronger greenhouse  
215 forcing in the former generates a larger signal-to-noise ratio (i.e. the magnitude of the forced  
216 precipitation response compared to that of natural internal variability) which aids the detection of  
217 the forced response.

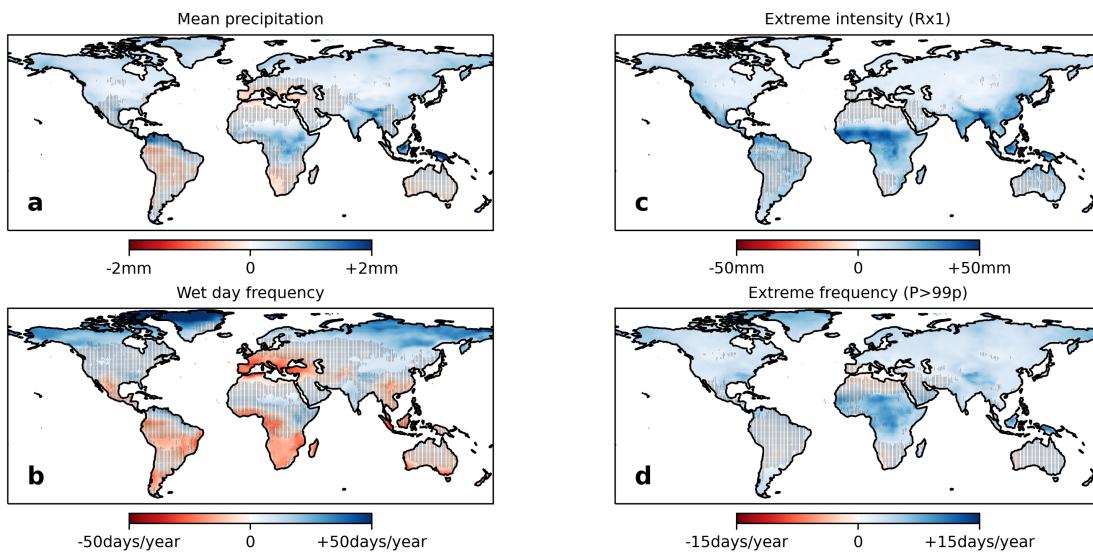


218 FIG. 2. The extent of inter-model agreement in the spatial pattern of forced precipitation change. The land  
219 area on which at least a certain percentage of models agree on the sign of forced change is shown for mean  
220 precipitation, the frequency of wet days, and the intensity (PX1) and frequency of daily extremes (P>99p). Results  
221 are shown having detected the forced response separately using low-frequency component analysis (LFC-1), and  
222 multi-decadal averages (10yr-av, 30yr-av).

223 Comparing the extent of agreement between detection methods, we find that using LFCA reduces  
224 inter-model discrepancies compared to taking decadal averages. These improvements are most  
225 considerable under the SSP126 forcing scenario, in which notable improvements are made even on  
226 a 30-year average. Assuming that inter-model agreement constitutes a benchmark of accuracy, this  
227 suggests that accounting for spatio-temporal correlations during detection via LFCA can improve

228 the accuracy with which a forced response is detected, and that these improvements are most  
229 considerable in contexts where the signal-to-noise ratio is low.

230 Despite these improvements, discrepancies between models in the sign of forced change persist.  
231 This is particularly so for changes in mean conditions, where high agreement (90% of models) is  
232 found on only 53 and 36% of land area for mean precipitation and wet day frequency under SSP585.  
233 By contrast high agreement is found on 77 and 65% of land area for the intensity and frequency of  
234 daily extremes under SSP585. The spatial distribution of these discrepancies is shown in Fig. 3  
235 overlain on maps of the ensemble mean forced response.



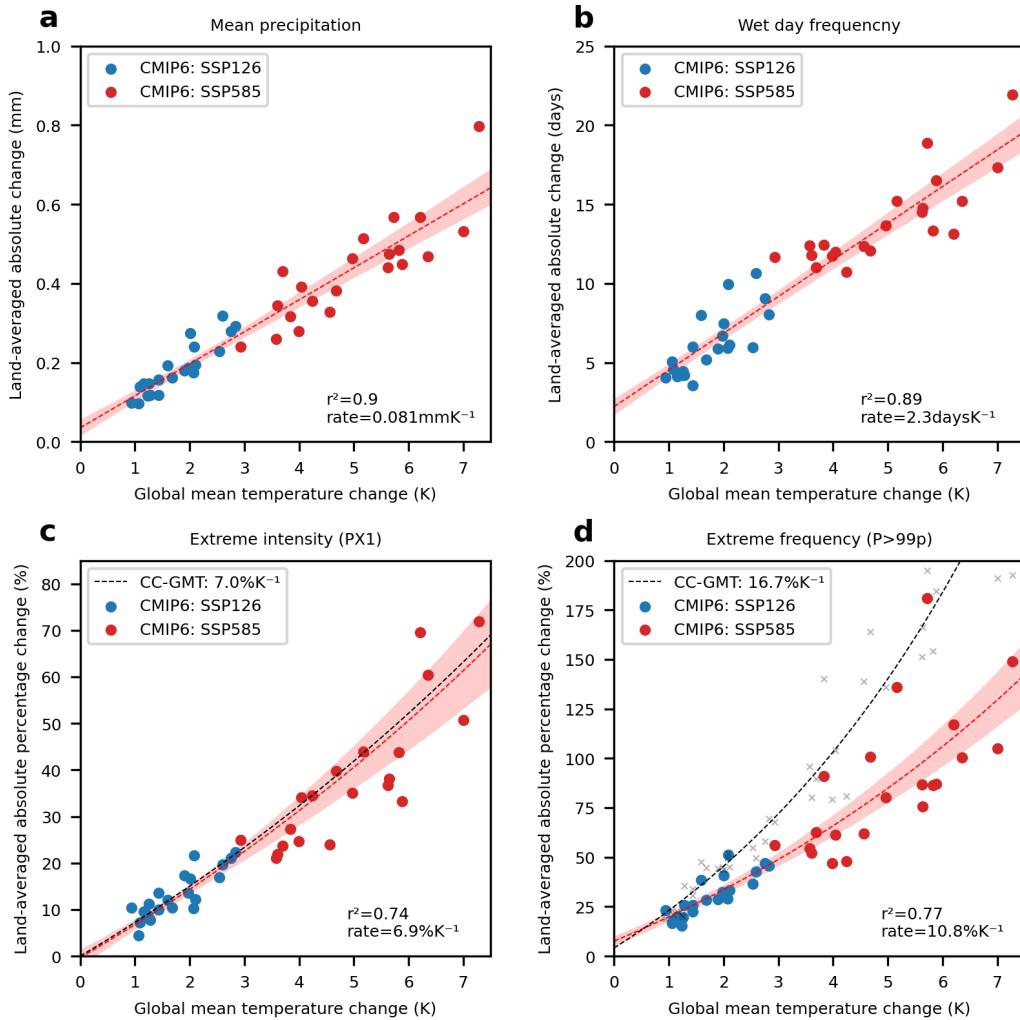
236 FIG. 3. The ensemble-mean forced response of mean daily precipitation (a), wet day frequency (b), and the  
237 intensity (c) and frequency (d) of daily extremes to SSP585 forcing. Forced changes are calculated with LFCA  
238 as described in the caption to Figure 1. Hatching indicates grid-cells in which less than 90% (19/21) of the  
239 ensemble agree on the sign of change.

240 The ensemble-mean forced response of precipitation (Fig. 1) resembles that identified by the  
241 IPCC (Masson-Delmotte et al. (2021)). Increases in mean precipitation across most of the global  
242 land mass contrast decreases across the Mediterranean basin, Central South America, and the  
243 southern tips of Africa and Australia. These changes reflect both a zonal intensification of the  
244 hydrological cycle (wet-get-wetter) (Marvel and Bonfils (2013)) and regional circulation changes  
245 (Chadwick et al. (2013)). The response of the number of wet days follows this pattern, but with

246 considerably more wide-spread regional reductions. This difference likely reflects the expected  
247 shift of the distribution of precipitation from relatively lighter to heavier events under global  
248 warming (Allen and Ingram (2002); Fischer and Knutti (2016)). The extreme indices demonstrate  
249 a response with more homogeneous increases, although some reductions are found. Reductions  
250 generally occur in regions of large mean precipitation decrease and large uncertainty, matching  
251 those identified by Pfahl et al. (2017) as having large dynamical contributions from circulation  
252 change which oppose the general thermodynamic increase in extreme precipitation.

253 *c. The magnitude of forced change - temperature-precipitation scaling across models*

254 Despite persistent uncertainty in the projected sign of regional precipitation change, we find  
255 that the average magnitude of such change scales strongly with GMT across all metrics (Fig. 4).  
256 To demonstrate this, we assess the land-area averaged (excluding Antarctica) absolute change in  
257 each precipitation metric from the forced response which we detect in each model, as well as the  
258 global-area averaged temperature change in each model estimated comparably using LFCA. Taking  
259 absolute values improves the correlations between precipitation and GMT change (compare Fig. 4  
260 to Fig. B1), considerably so for mean precipitation and the frequency of wet days. This suggests that  
261 when shifting atmospheric currents contribute large uncertainty to the sign of regional precipitation  
262 change, the intensity of these changes can still be closely related to the underlying thermodynamic  
263 driver. We note that taking absolute values is a similar approach to that used by Chadwick  
264 et al. (2016), who assess the percentage of tropical land area projected to experience considerable  
265 precipitation (>20%) of either positive or negative sign. Our method offers a complementary  
266 perspective by assessing the average magnitude of change across all land-areas in multiple metrics.



267 FIG. 4. The scaling of land area-averaged absolute precipitation change with global mean temperature (GMT)  
 268 across CMIP6 models and scenarios. Forced changes between 1950-1960 and 2090-2100 are calculated from  
 269 the lowest-frequency component of each precipitation index (as in Fig. 1) and of annual mean temperature.  
 270 Red and blue colors denote the SSP585 and SSP126 scenarios of future greenhouse forcing. The results of  
 271 least-squares linear regressions are shown in dashed red with the 5<sup>th</sup> and 95<sup>th</sup> confidence intervals shaded  
 272 based on bootstrapped estimates of the regression (1000 climate model resamples with replacement). Changes  
 273 in extreme metrics are calculated as a percentage of the historical baseline (1850-1950) for comparison to the  
 274 theoretical expectations of the Clausius-Clapeyron relation, shown in dashed black lines. For the frequency  
 275 of daily extremes ( $P > 99p$ ), the CC relation is estimated by scaling up each day of the historical precipitation  
 276 distribution (1850-1950) by the given level of GMT change, and re-calculating each index, following Fischer  
 277 and Knutti (2016). Individual estimates from this method are shown in grey, the black dashed-line showing the  
 278 result of an exponential regression to these estimates. The resulting theoretical scaling rate of this regression is  
 279 displayed in the figure legend.

280 We express changes in the extreme metrics in terms of percentages from the historical base-  
281 line (1850-1950, percentages calculated at the grid-cell before spatial aggregation) in order to  
282 compare them to the theoretical expectations of the Clausius-Clapeyron (CC) relation. We find  
283 that the intensity of extremes follow this behaviour closely, increasing at a rate of  $6.9\%K^{-1}$ . For  
284 the frequency of daily extremes, we follow Fischer and Knutti (2016) to estimate a theoretical  
285 thermodynamic scaling. We apply the CC relation for a given GMT change to each day of the  
286 historical precipitation distribution (1850-1950) and then re-calculate the indices on the re-scaled  
287 distribution. This predicts a considerably higher scaling of  $16.7\%K^{-1}$ . Although, we observe a  
288 larger scaling for the frequency rather than the intensity of extremes, it falls short of this expected  
289 scaling at  $10.8\%K^{-1}$ .

#### 290 *d. Temperature-precipitation scaling within models*

291 Furthermore, we exploit the detection of a forced precipitation response within each individual  
292 CMIP-6 model to assess the scaling of precipitation and GMT change within individual models.  
293 To do so, we use changes in the time-varying forced response of precipitation and temperature  
294 occurring over pairs of non-overlapping decades separated by 25 year periods within each climate  
295 model. This approach reveals robust temperature-precipitation scaling relationships which are  
296 clearly identifiable within each climate model, and which can explain a large proportion of the  
297 inter-temporal changes in precipitation (Fig. 5). Considerable improvements in the robustness of  
298 these estimates are made when first filtering with LFCA compared to using the raw CMIP data, in  
299 particular for mean precipitation and the number of wet days. Using LFCA, the  $R^2$  of the identified  
300 relations increase from median values of 64, 4, 77 and 82% to 84, 76, 84 and 93% for mean  
301 precipitation, wet day frequency and the intensity and frequency of daily extremes respectively  
302 (see Figs. B6-B9 for the scalings identified without LFCA).

313 On average, the rates at which precipitation changes scale with GMT within individual models  
314 is consistent with that identified between models (Fig. 6), other than for the frequency of extremes  
315 for which a considerably larger scaling is observed on average within models (15.21%) which  
316 has closer consistency to the expected CC-scaling . However, there is considerable inter-model  
317 heterogeneity in these rates, the distribution of which is shown in Fig. 6. We estimate coefficients of  
318 variation of 21, 19, 39 and 28% for the distributions for mean precipitation, wet day frequency and  
319 the intensity and frequency of daily extremes. This demonstrates that large inter-model uncertainty  
320 exists in the modelled rate at which precipitation changes scale with temperature. Moreover, the  
321 inter-model differences in intra-model scaling rates are significantly different from zero at the 5%  
322 level given our methodological uncertainty (estimated using 1000 bootstrapped replacements of  
323 the inter-temporal changes in the regressions estimated in Fig. 5) for 37, 29, 56 and 61% of unique  
324 model pairs for mean precipitation, the number of wet days and the intensity and frequency of  
325 extremes respectively. As such we can conclude that there are significant inter-model differences  
326 in the rates at which precipitation scales with GMT, particularly for the scaling of extremes. These  
327 differences contribute to uncertainty in the projections of future precipitation change, and their  
328 identification therefore offers the opportunity to constrain such uncertainties. One potential avenue  
329 to do so could be the use of observational estimates of the rate of these scalings to constrain  
330 multi-model ensemble projections.

331 Exploring the source of these diverging precipitation scaling rates is beyond the scope of this  
332 analysis, but we note that there is clear co-variation between the GMT-scaling rates of mean  
333 precipitation and both of the extreme metrics across models (Fig. B10). This suggests that common  
334 physical mechanisms may underlie the model biases in the rates at which these precipitation  
335 characteristics scale with GMT.

#### 343 **4. Discussion and concluding remarks**

344 Our work sheds light on a number of challenges relating to the uncertainty of future precipitation  
345 projections. First, we demonstrate that the use of a pattern-filtering technique, LFCA, can improve  
346 the accuracy with which the spatial patterns of anthropogenically-forced precipitation change are  
347 projected by limiting the obscuring role of internal variability, in particular in the context of low  
348 signal-to-noise ratios. However, considerable uncertainties persist, reflecting the discrepancies

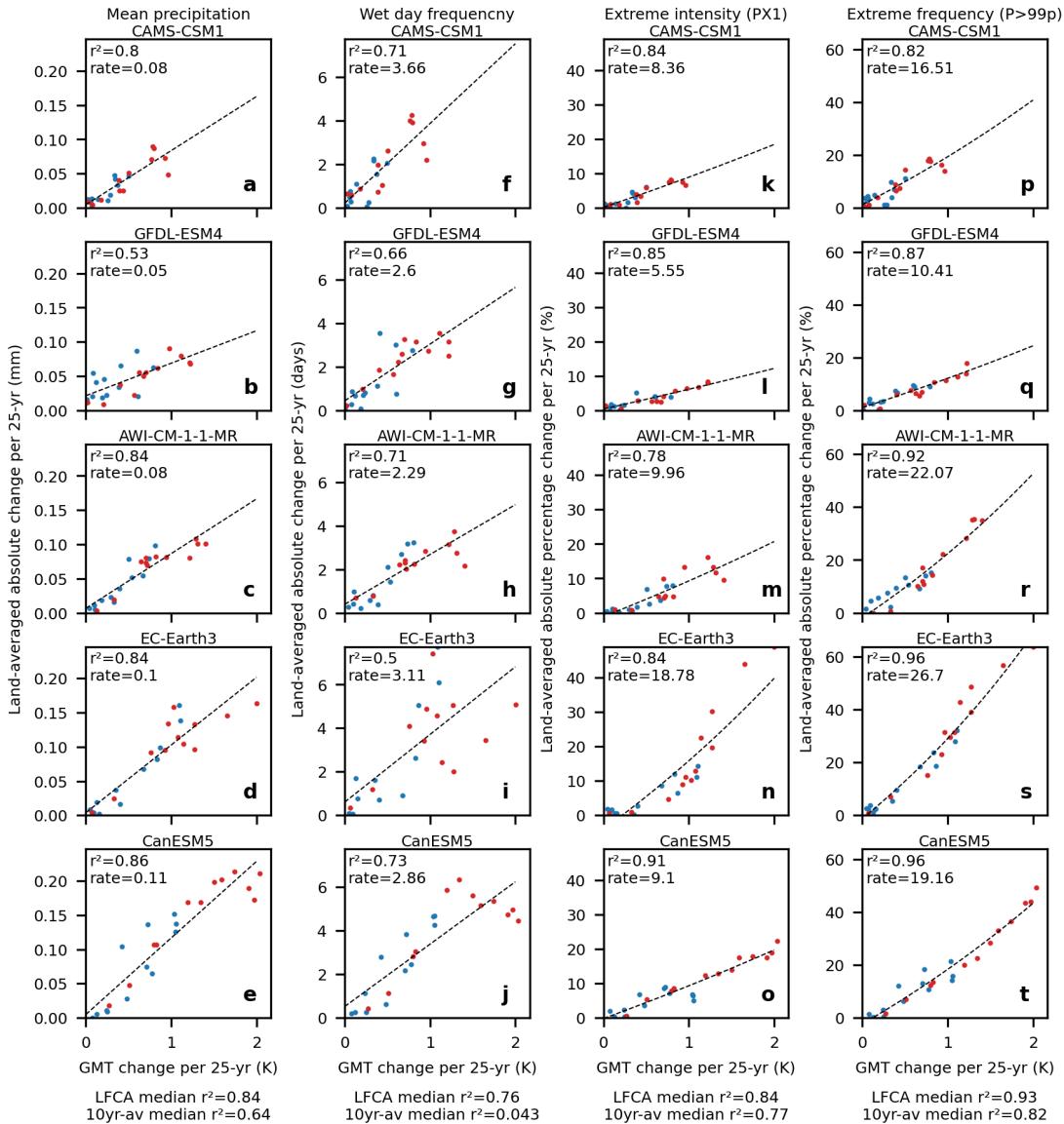
349 inherent in the modelling of physical processes within different climate models. Previous work  
350 suggests that the dynamical contribution from atmospheric circulation change is the major source  
351 of these uncertainties (Shepherd (2014); Kent et al. (2015); Pfahl et al. (2017)), and continued  
352 work to understand and reduce them is crucial.

353 Despite these uncertainties, our analysis demonstrates that the magnitudes of precipitation change  
354 are closely constrained by changes in GMT. While the scaling of precipitation extremes with GMT  
355 across climate models has already been studied, such robust scaling of changes in mean conditions  
356 have not previously been identified. Our approach taking absolute values of regional change  
357 contributes considerably to revealing these relations. This approach relates closely to that of  
358 Chadwick et al. (2016), but demonstrates precipitation-GMT scaling for the magnitude rather  
359 than extent of change, and considers multiple metrics across the global land area rather than  
360 averages across the tropics. The fact that these relations are improved when taking absolute  
361 values, and most considerably so for the metrics in which dynamical changes from atmospheric  
362 circulation contribute large uncertainty to the sign of regional change, suggests that the intensity  
363 of such dynamical changes may also be well constrained by the underlying thermodynamic driver  
364 of climatic change i.e. GMT. The observed dependence of shifting atmospheric circulation on  
365 changes to sea surface temperature and land-sea temperature-gradients (Deser and Phillips (2009);  
366 Chadwick et al. (2013, 2014); Ma and Xie (2013)) may support such an interpretation, but further  
367 analysis in this regard is beyond the scope of the present work. Regardless, these relations suggest  
368 that uncertainty in the magnitude of regional precipitation change is closely tied to uncertainty in  
369 the equilibrium climate sensitivity and GMT change.

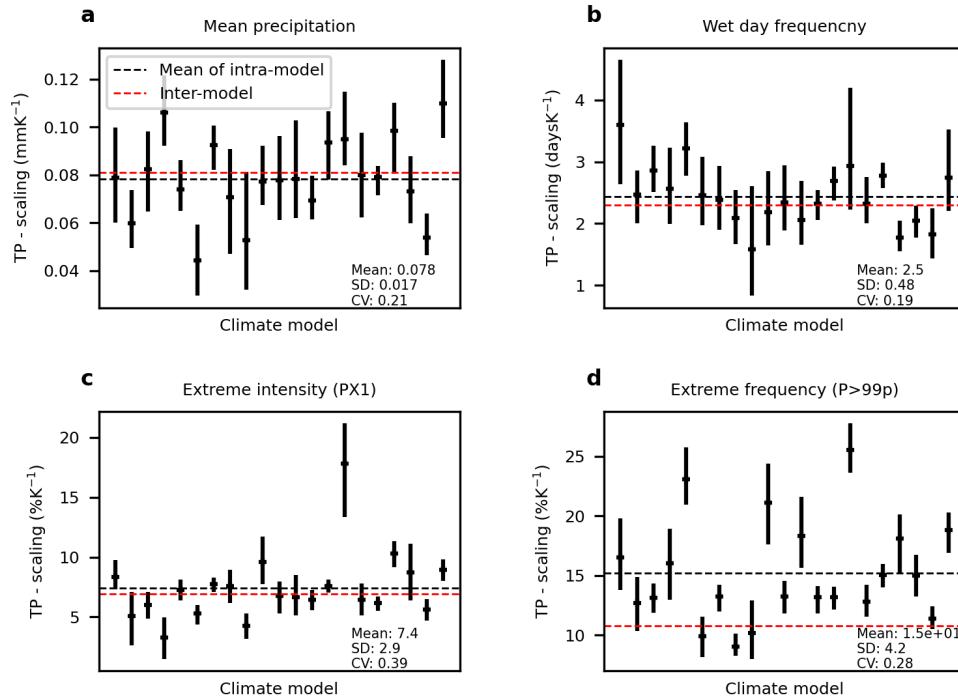
370 Furthermore, by identifying these scaling relations clearly within individual climate models,  
371 we are able to diagnose a source of the uncertainty in the magnitude of projected precipitation  
372 change, in addition to that arising from uncertainty in GMT. The rates at which precipitation  
373 scales with GMT differ considerably and significantly between models, and this could present  
374 opportunities to constrain the magnitude of future projections by their comparison to estimates of  
375 such scalings from observations. Accurate observational estimates may be challenging to obtain  
376 given a relatively short historical record during which different components of anthropogenic  
377 forcing (aerosol, greenhouse) may confound one another, amongst other challenges (Williamson  
378 et al. (2021)). Nevertheless, observational constraints on precipitation have shown some success

379 (O’Gorman (2012); Shiogama et al. (2022); Schewe and Levermann (2022)), and the clear signal of  
380 intensification of precipitation extremes in the historical record may suggest that such scalings are  
381 indeed accurately identifiable (Min et al. (2011); Zhang et al. (2013); Fischer and Knutti (2016);  
382 Chen and Sun (2017); Kirchmeier-Young and Zhang (2020); Madakumbura et al. (2021)). Analyses  
383 of precipitation extremes in Europe suggest that CMIP models may strongly under-estimate the  
384 observed change for a given level of warming (Fischer and Knutti (2016); Myhre et al. (2019)),  
385 emphasising that constraining such projections in this way may be critical.

386 Finally, the demonstrated constraints on the magnitude of future precipitation change may be  
387 useful for global risk and impact assessments. Accurate information on the sign and magnitude  
388 of regional changes is undoubtedly of the greatest value, but in the absence of the former a  
389 constraint on the latter may provide some complementary information. For example, global risk  
390 assessments may find utility in constraints on the global average magnitude of expected impacts  
391 from precipitation changes e.g. in terms of how they compare to impacts from other aspects of  
392 climate change (such as from temperature) or to other socio-economic events such as pandemics,  
393 wars or financial crises. Moreover, the demonstration of such robust scalings may support the use  
394 of pattern scaling techniques (Herger et al. (2015)) in the projection of precipitation impacts. This  
395 would constitute a key step within the complex chain linking emissions, to GMT change, to the  
396 impacts arising from regional precipitation change (Kotz et al. (2022)).



303 FIG. 5. The scaling of the land-area averaged absolute change of precipitation characteristics with global  
 304 mean temperature (GMT) change within individual CMIP6 climate models. A selection of models are shown  
 305 for simplicity, but results for the full ensemble can be seen in Figs. B2-5. Forced changes are calculated from  
 306 the lowest-frequency component detected with low-frequency component analysis, and the scalings identified  
 307 from changes between pairs of non-overlapping decades separated by 25 years. Red and blue colors denote the  
 308 SSP585 and SSP126 scenarios of future greenhouse forcing and in black the results of a least-squares regression  
 309 are shown. Models are ordered (a-u, top-left to bottom-right) from lowest to highest GMT change as in Fig.  
 310 1. The median  $R^2$  obtained across climate models is indicated at the bottom of each column, having detected  
 311 the forced changes using either LFCF or decadal averages. See Figs. B6-9 for the results without having first  
 312 applied LFCF.



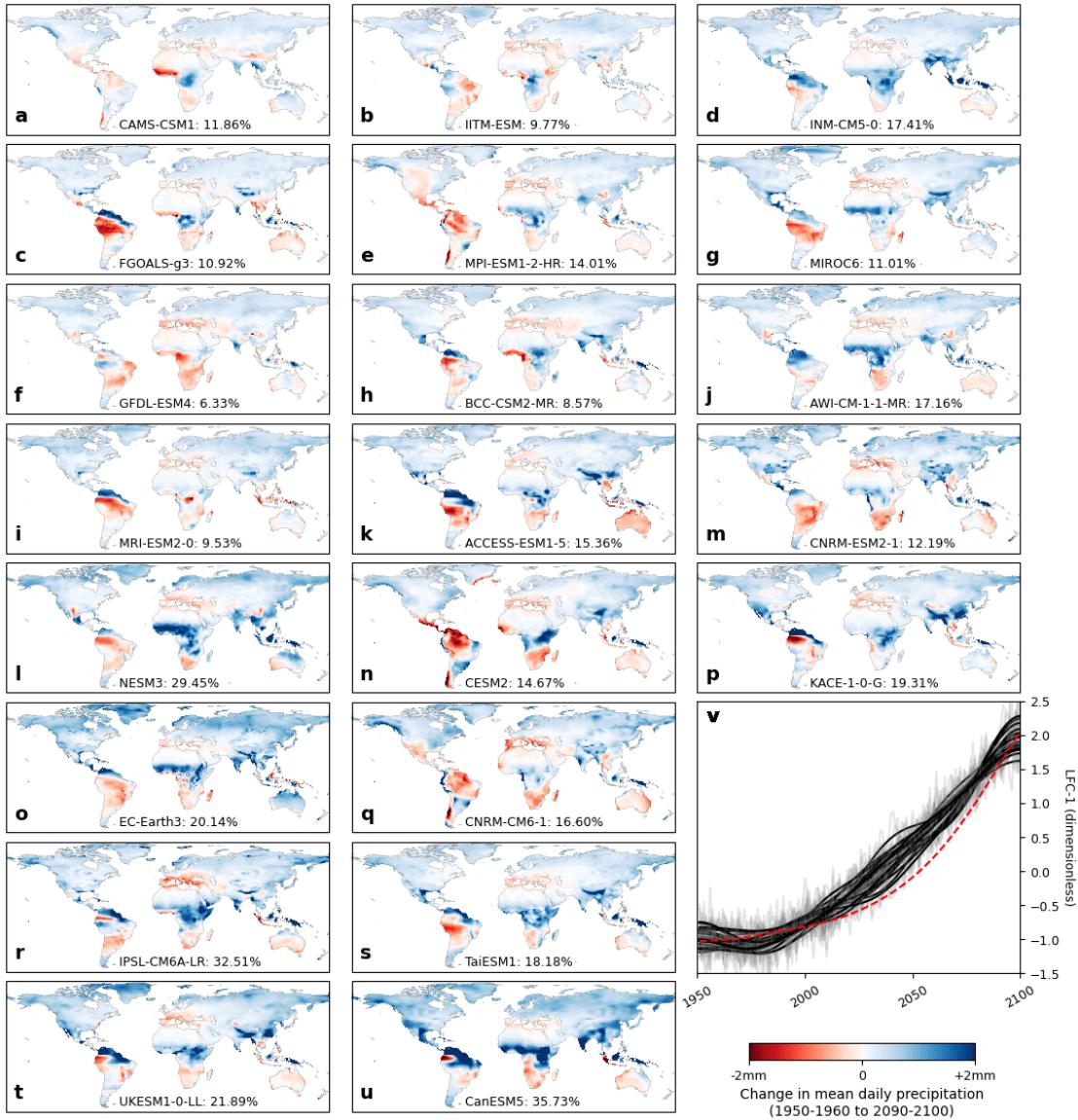
336 FIG. 6. Inter-model spread in the temperature-precipitation scaling relationships identified from the forced  
 337 changes detected within individual CMIP6 models, for (a) mean precipitation, (b) wet day frequency and (c) the  
 338 intensity (Px1) and (d) frequency (P>99p) of daily extremes. 10% confidence intervals of the scaling within  
 339 each model are obtained by boot-strapping the regressions shown in Fig. 5, and displayed as vertical bars. The  
 340 mean of the within-model scalings (as identified in Fig. 5) and the between-model scalings (as identified in Fig.  
 341 4) are displayed by the horizontal dashed lines in black and red respectively. The mean, standard deviation, and  
 342 coefficient of variation of the intra-model scalings across models are also displayed numerically.

397 *Acknowledgments.* MK and LW received funding from the Volkswagen foundation. SL received  
398 funding from the German Research Foundation (DFG, project number 427397136) and from the  
399 German Federal Ministry of Education and Research (BMBF, project number 01LP1907A). AL  
400 received funding from the Horizon 2020 Framework Programme of the European Union (grant  
401 agreement number 820712).

402 *Data availability statement.* Raw CMIP6 data is available from [https://esgf-](https://esgf-node.llnl.gov/projects/cmip6/)  
403 [node.llnl.gov/projects/cmip6/](https://esgf-node.llnl.gov/projects/cmip6/). Code for low-frequency component analysis is available  
404 from <https://github.com/rcjwills/lfca>. All other data and code is available from the authors upon  
405 request.

## 406 APPENDIX A

### 407 **Forced response detected with LFCA**



408 FIG. A1. The detected forced response of mean precipitation under historical and SSP585 scenario greenhouse  
 409 forcing. As Fig. 1 but for all models in the CMIP6 ensemble. Models are ordered a-u in order of increasing  
 410 GMT change.

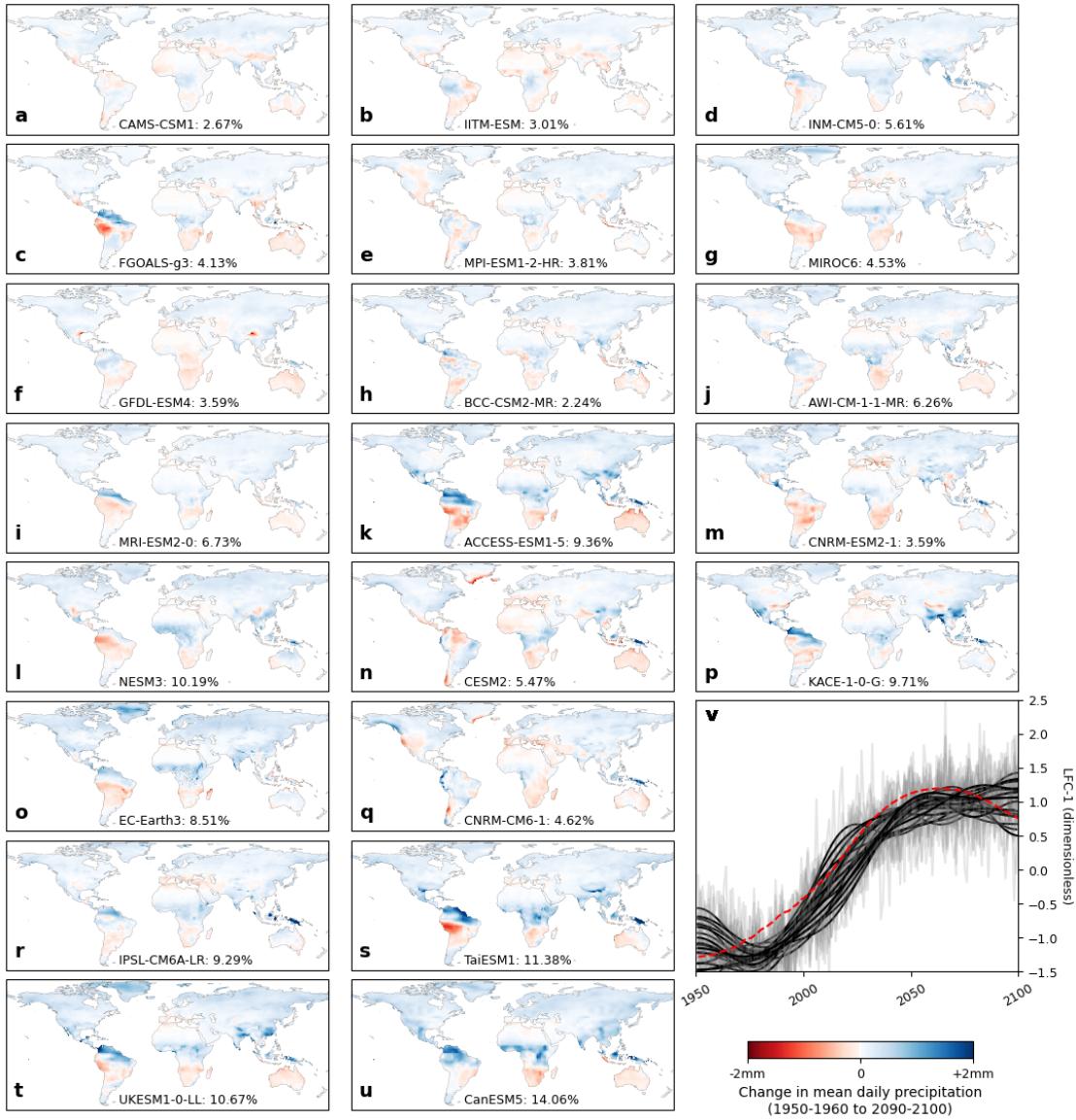
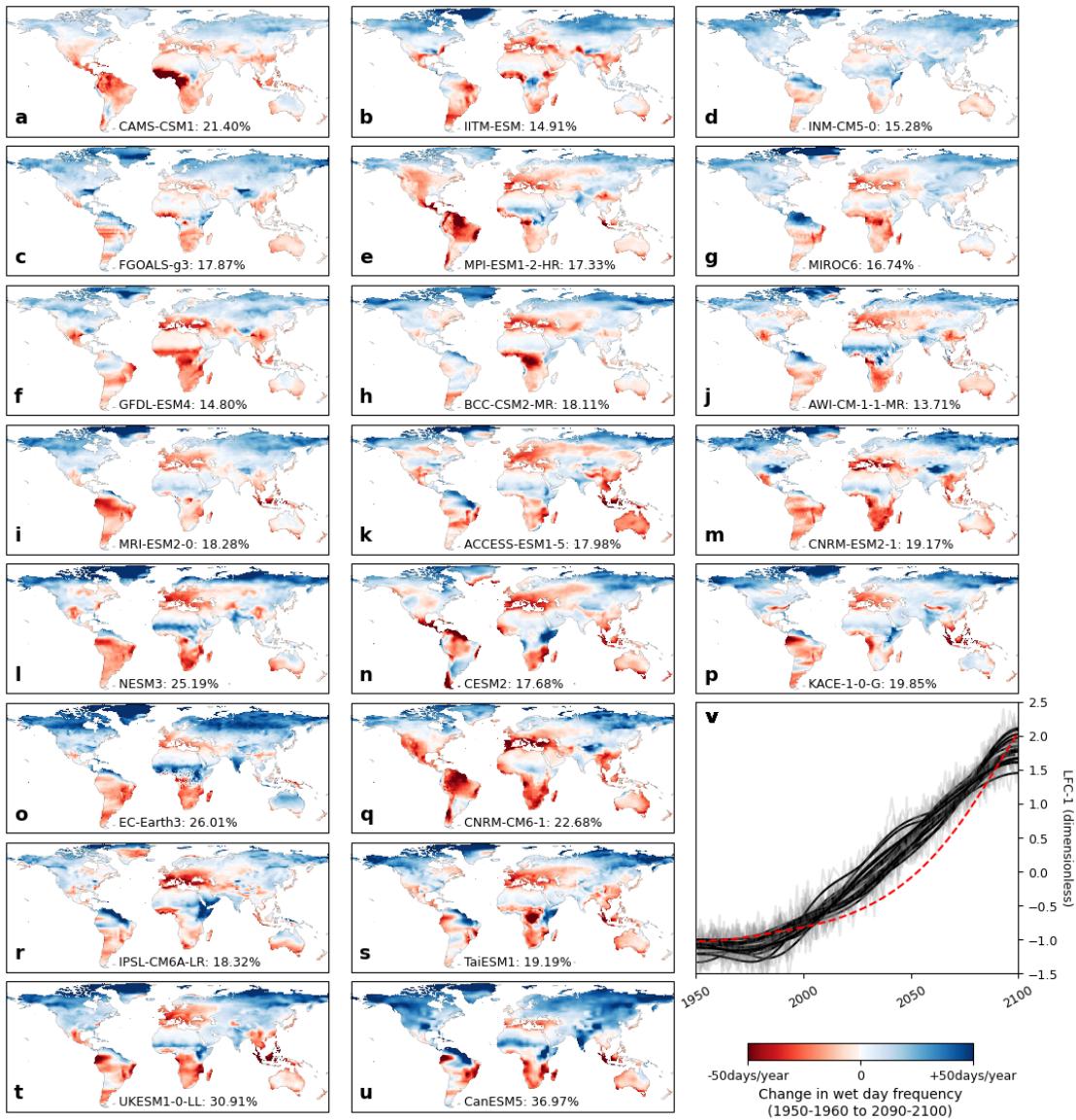


FIG. A2. As Fig. A1 but under the historical and SSP126 scenario greenhouse forcing.



411 FIG. A3. The detected forced response of the wet day frequency under historical and SSP585 scenario  
 412 greenhouse forcing. As Fig. 1 but for all models in the CMIP6 ensemble. Models are ordered a-u in order of  
 413 increasing GMT change.

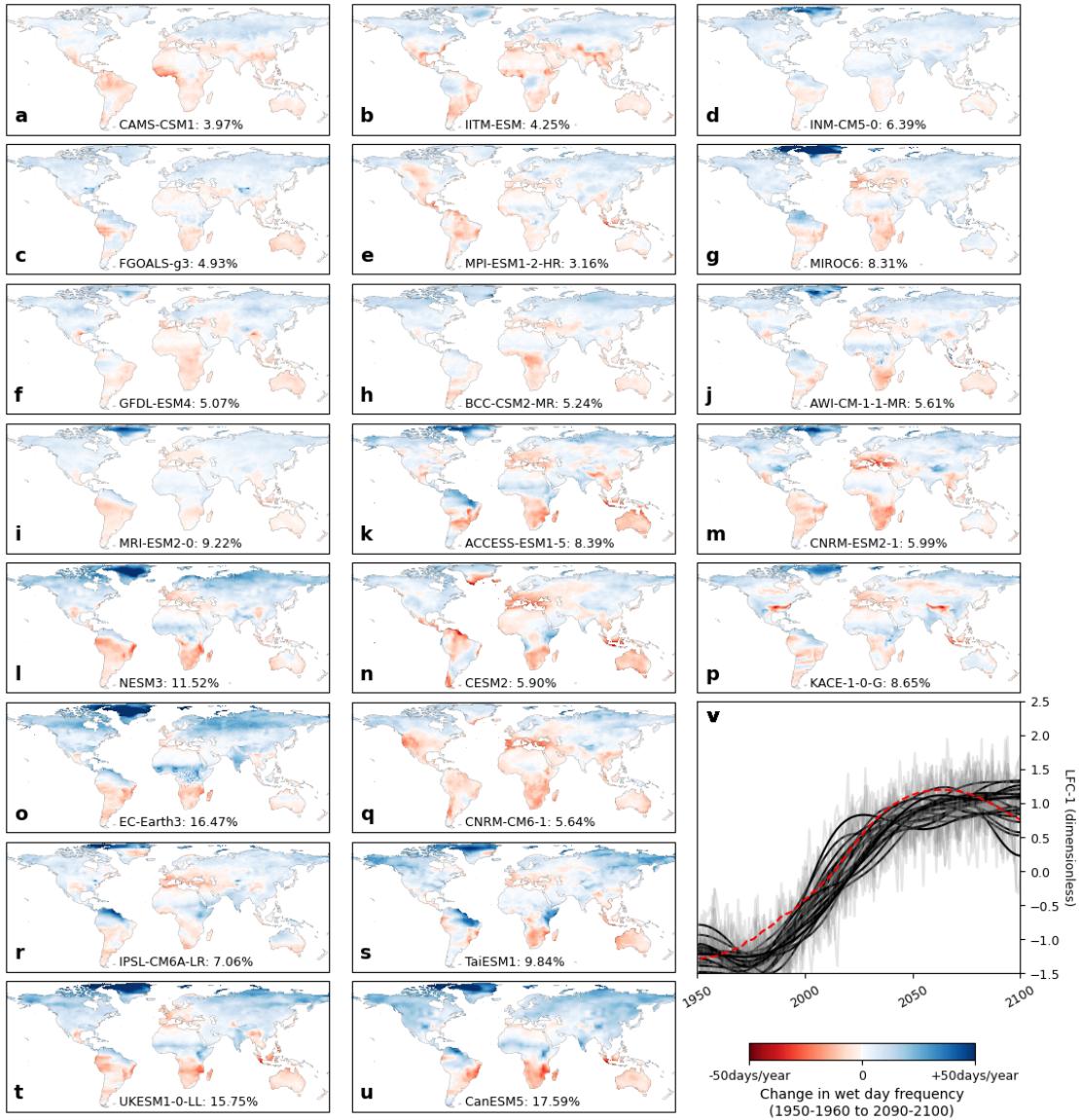
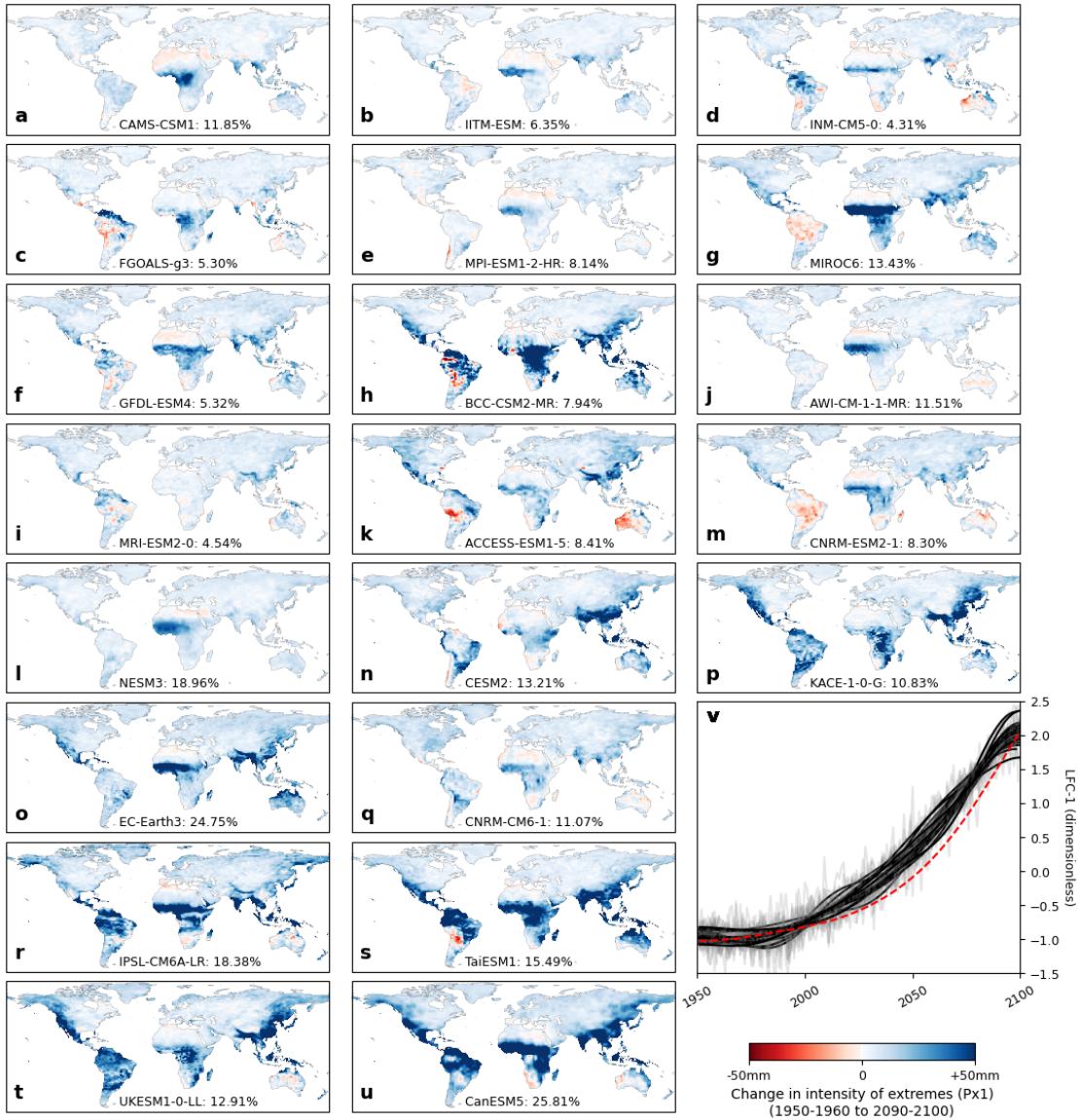


FIG. A4. As Fig. A3 but under the historical and SSP126 scenario greenhouse forcing.



414 FIG. A5. The detected forced response of the intensity of daily extremes under historical and SSP585 scenario  
 415 greenhouse forcing. As Fig. 1 but for all models in the CMIP6 ensemble. Models are ordered a-u in order of  
 416 increasing GMT change.

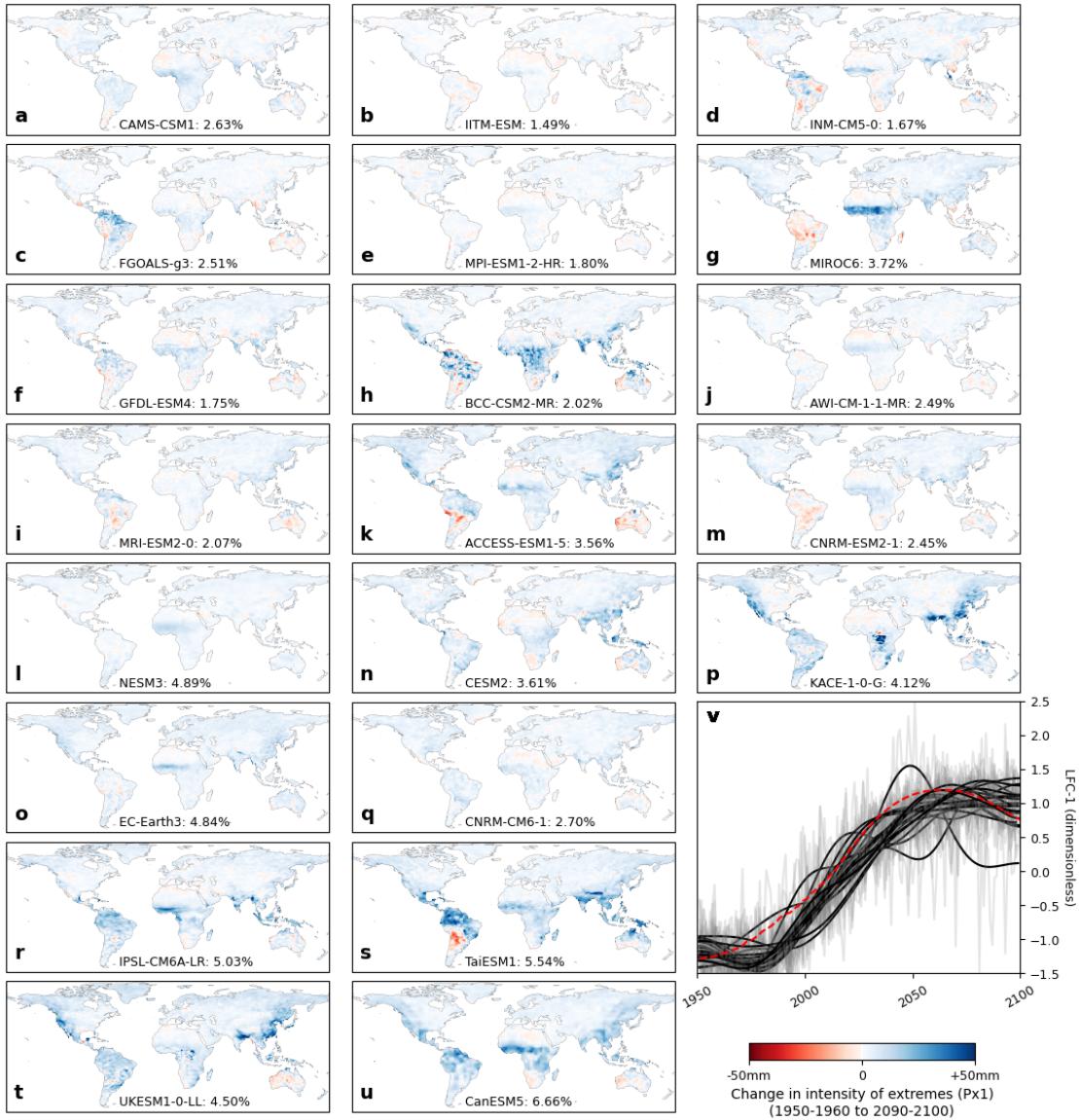
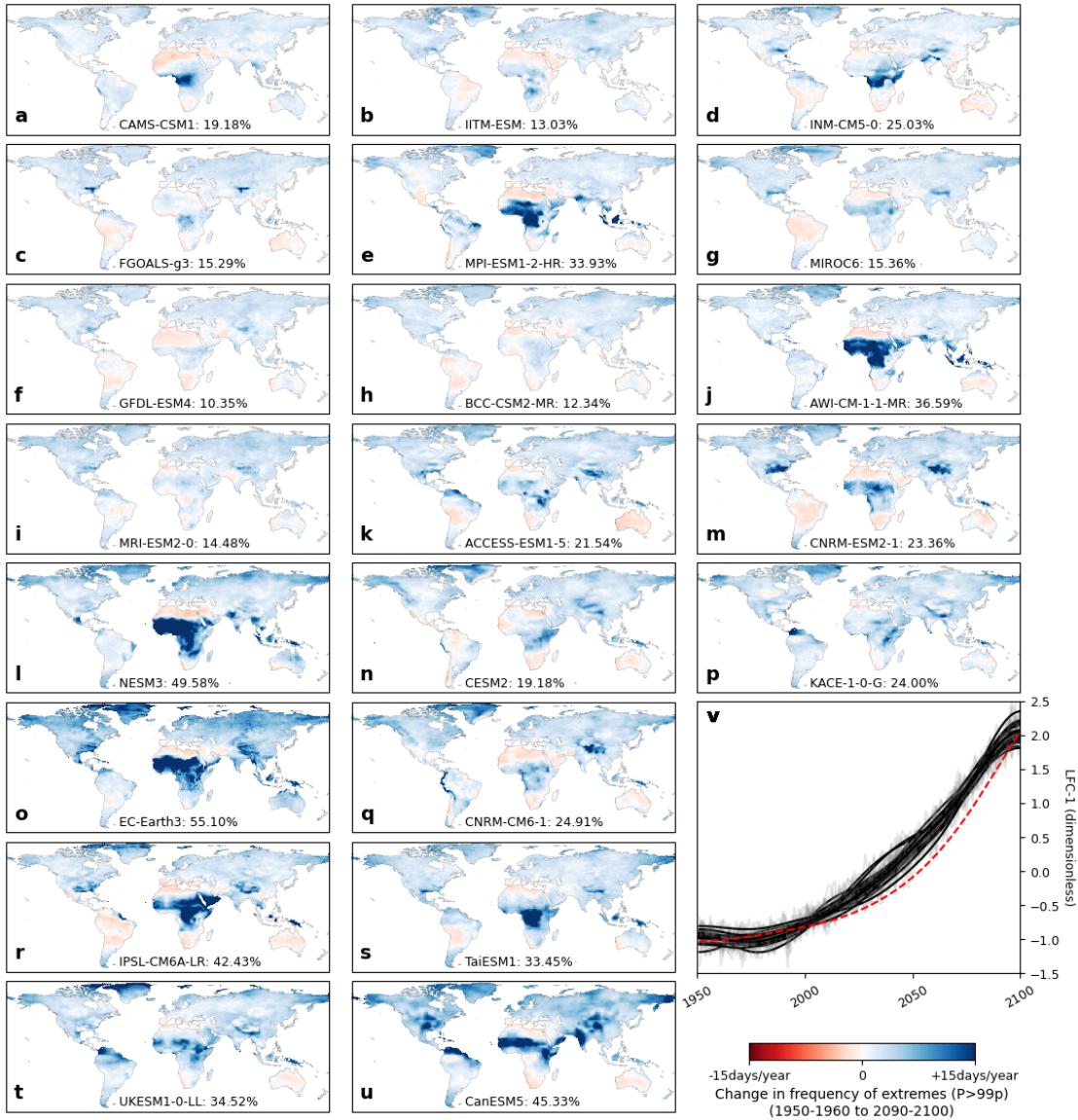


FIG. A6. As Fig. A5 but under the historical and SSP126 scenario greenhouse forcing.



417 FIG. A7. The detected forced response of the frequency of daily extremes under historical and SSP585 scenario  
 418 greenhouse forcing. As Fig. 1 but for all models in the CMIP6 ensemble. Models are ordered a-u in order of  
 419 increasing GMT change.

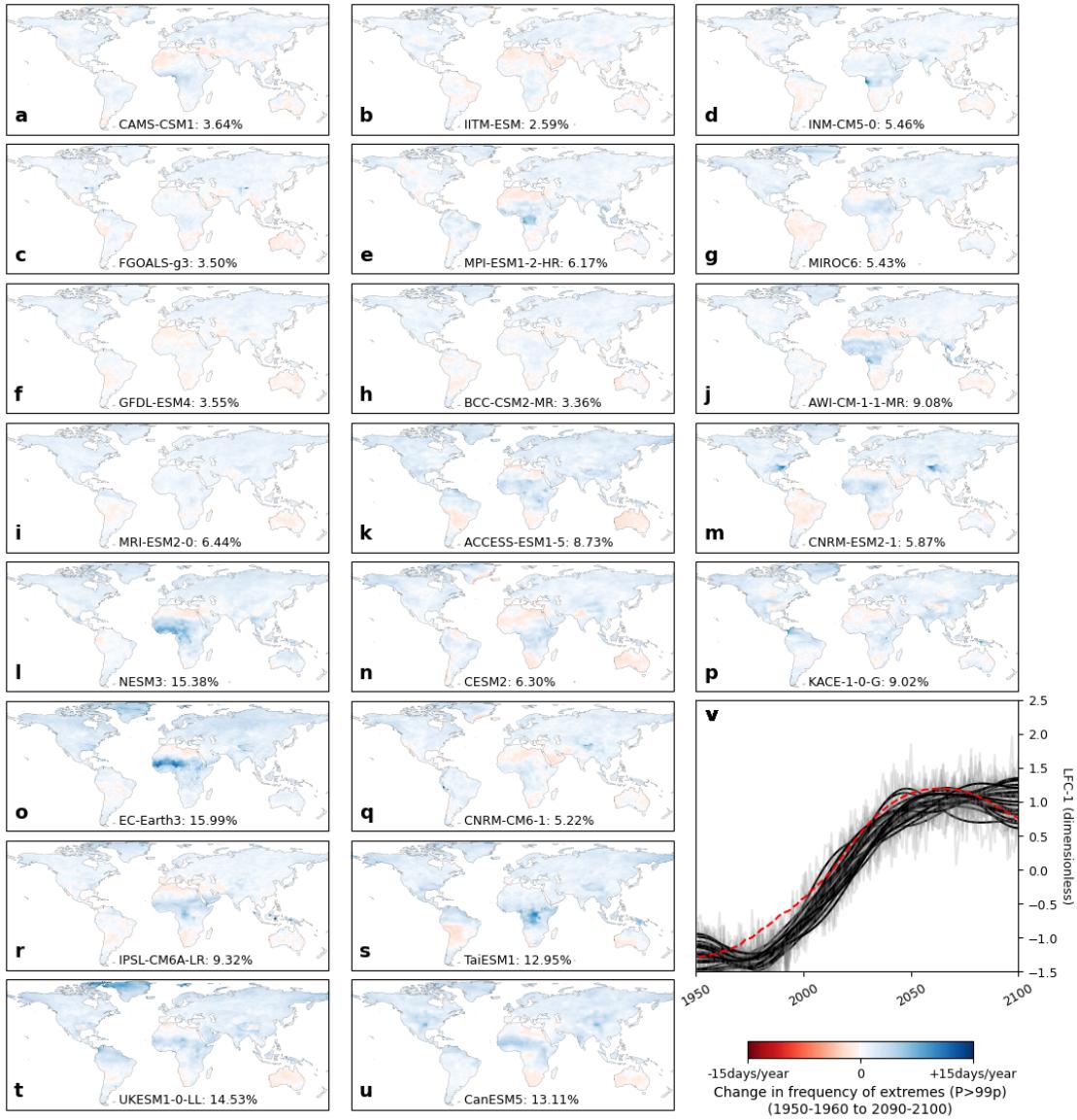
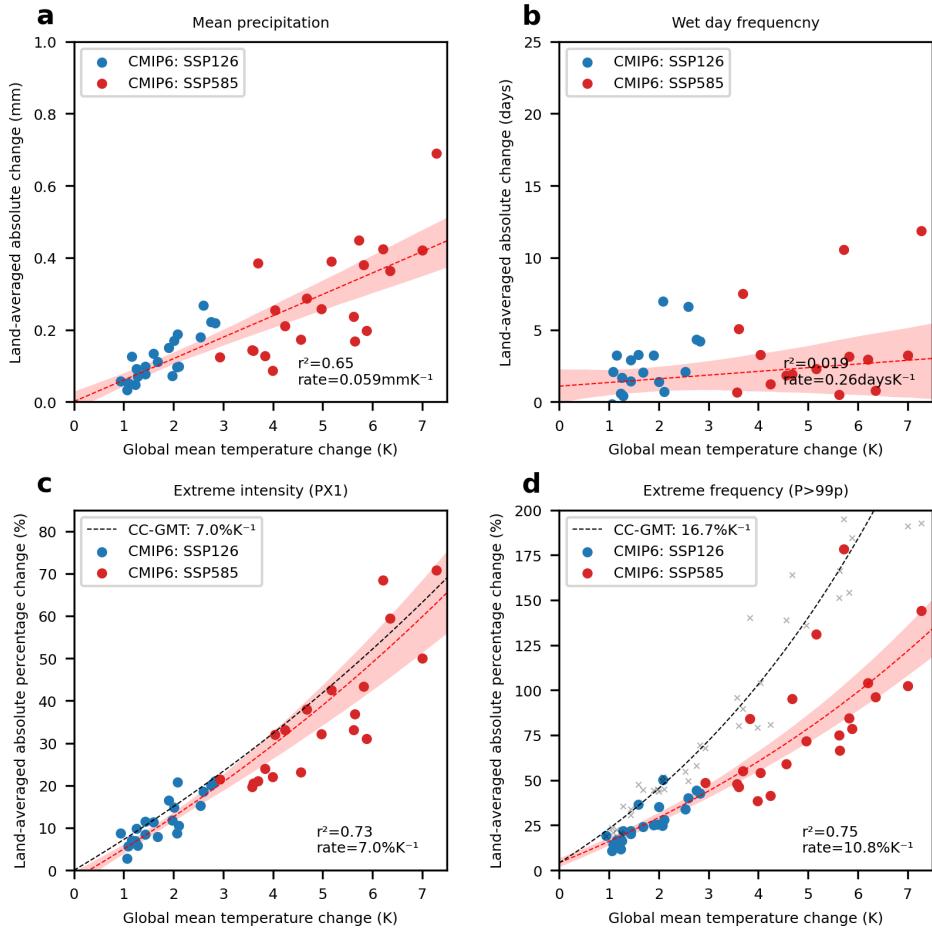
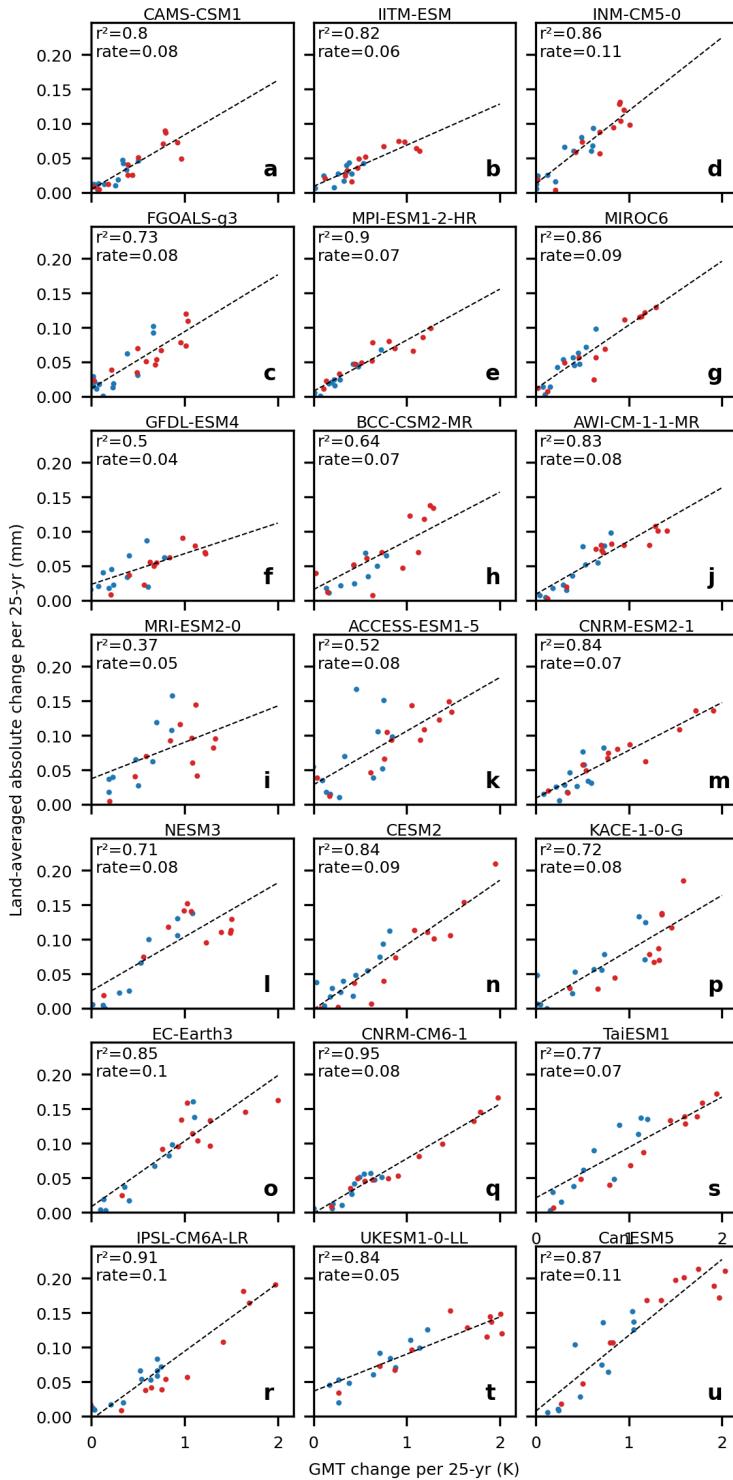


FIG. A8. As Fig. A7 but under the historical and SSP126 scenario greenhouse forcing.

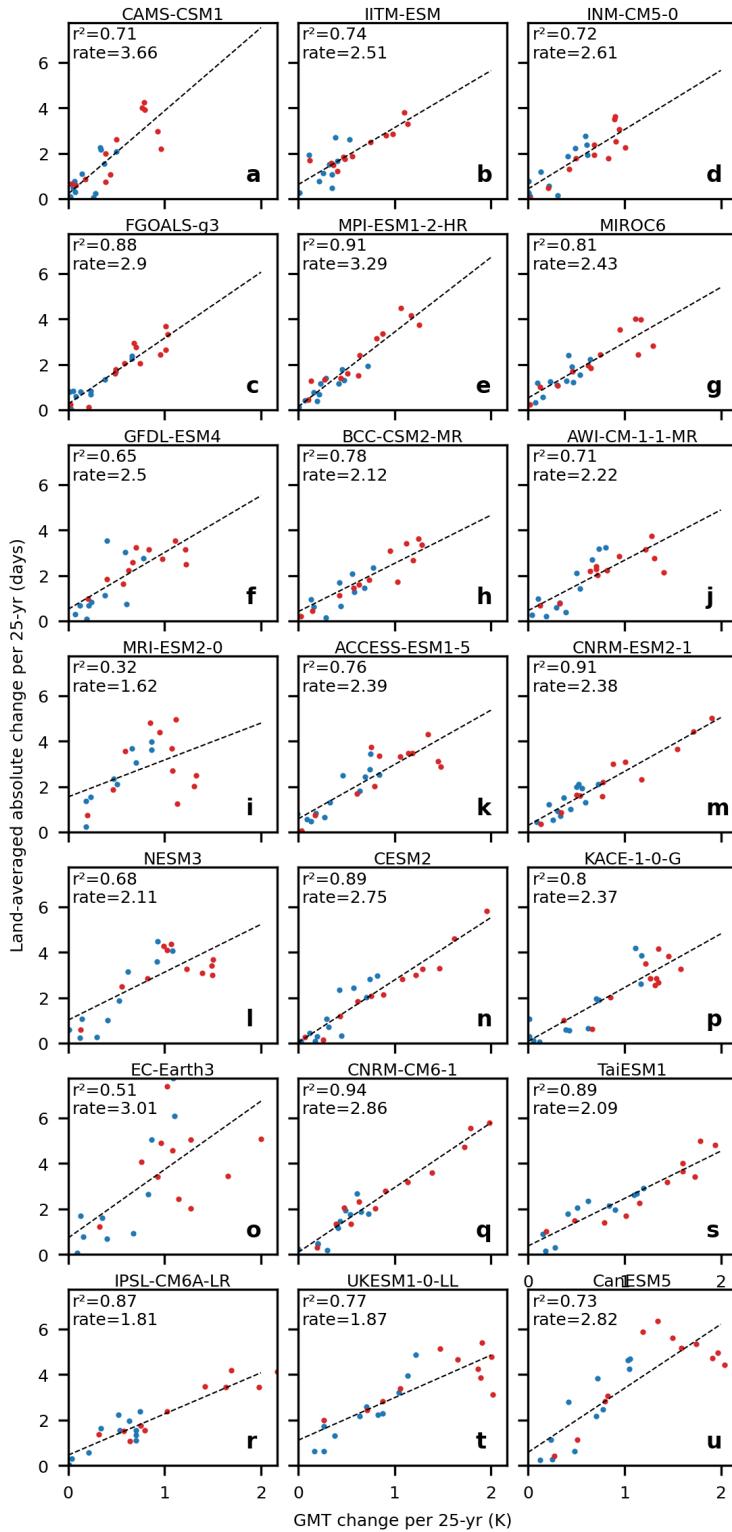
**Temperature-precipitation scaling**



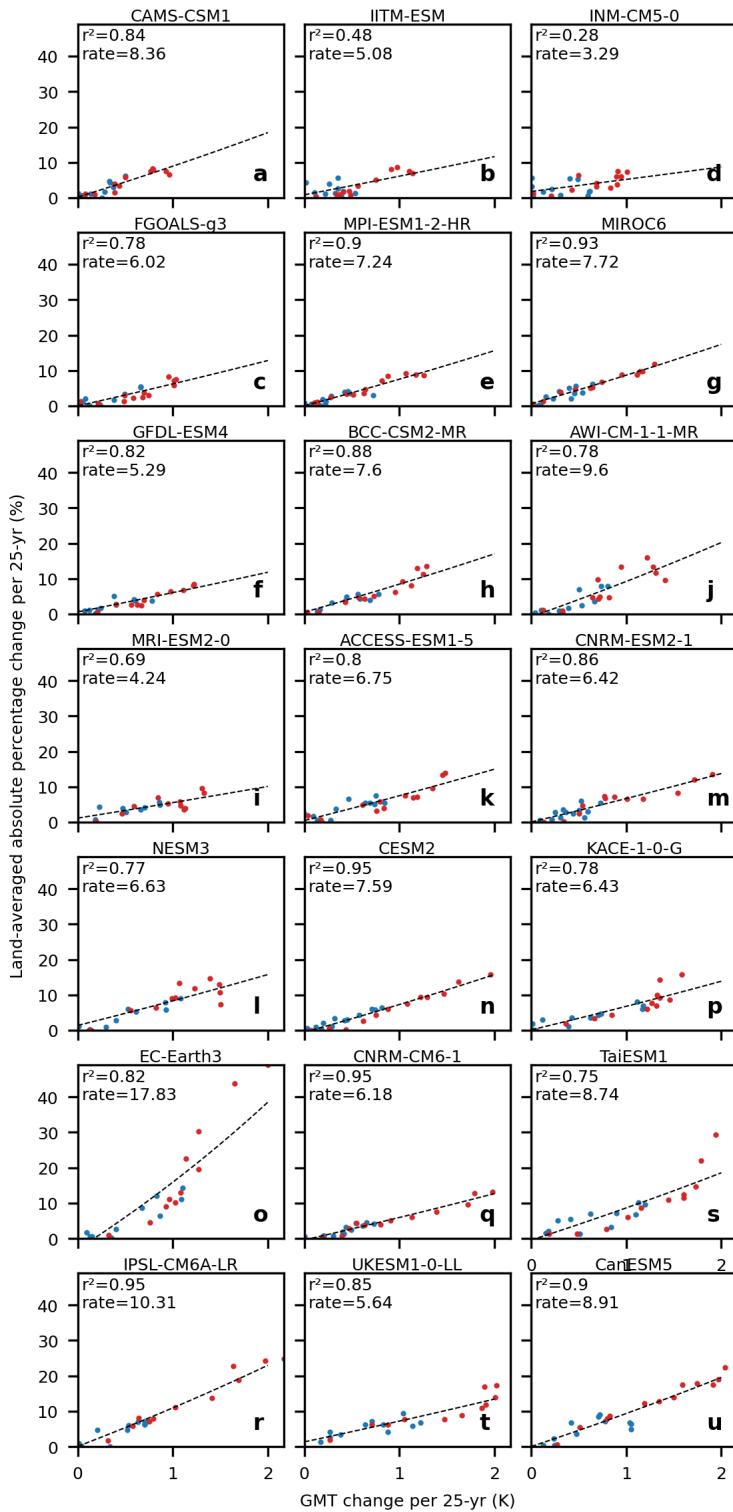
422 FIG. B1. Scaling between precipitation changes and GMT change without taking absolute values. As Fig. 4  
 423 but without taking absolute values of regional precipitation change.



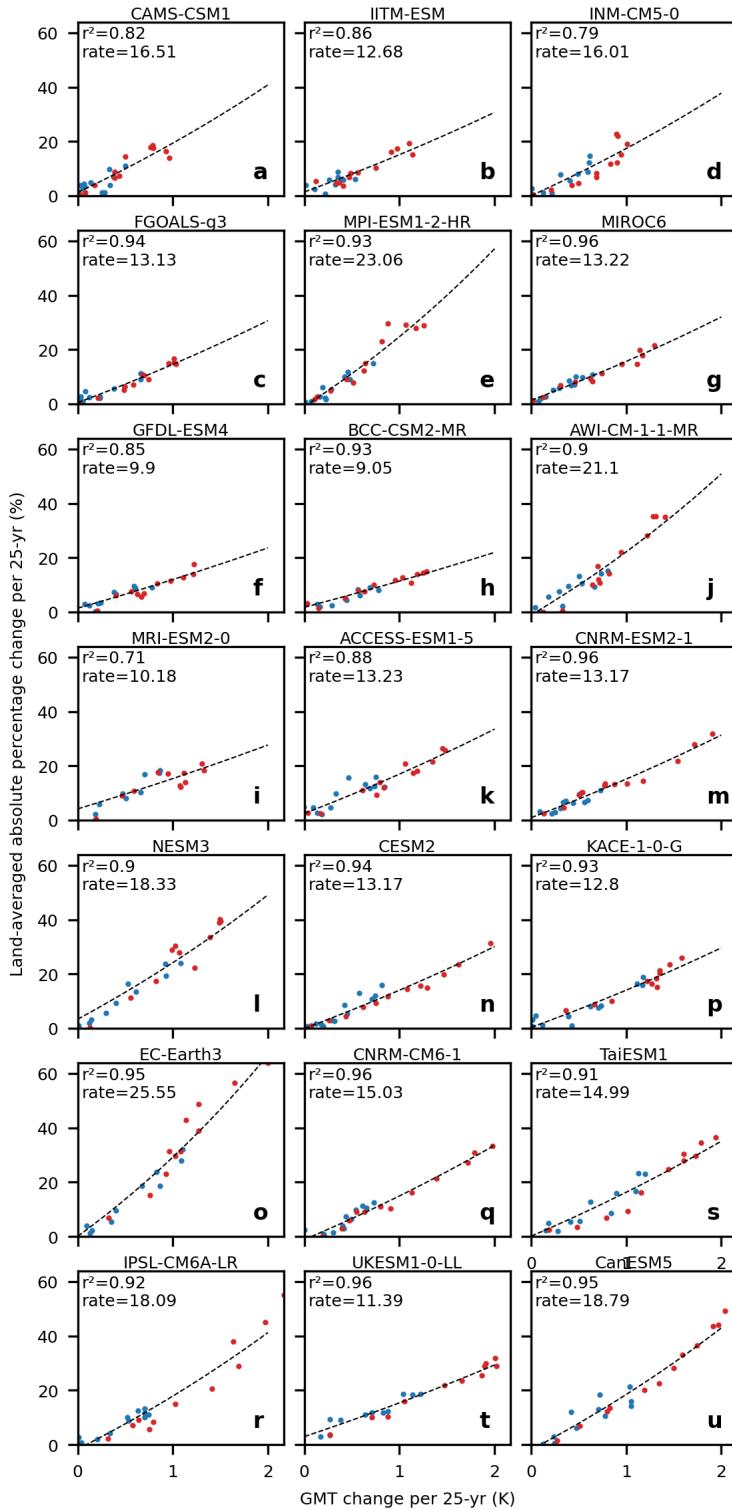
424 FIG. B2. Intra-model scaling between mean precipitation and GMT change for all members of the CMIP6  
 425 ensemble. As Fig. 5a-e but for all members.



426 FIG. B3. Intra-model scaling between wet day frequency and GMT change for all members of the CMIP6  
 427 ensemble. As Fig. 5f-j but for all members.



428 FIG. B4. Intra-model scaling between the intensity of daily extremes (PX1) and GMT change for all members  
 429 of the CMIP6 ensemble. As Fig. 5k-o but for all members.



430 FIG. B5. Intra-model scaling between the frequency of daily extremes ( $P > 99p$ ) and GMT change for all  
 431 members of the CMIP6 ensemble. As Fig. 5p-t but for all members.

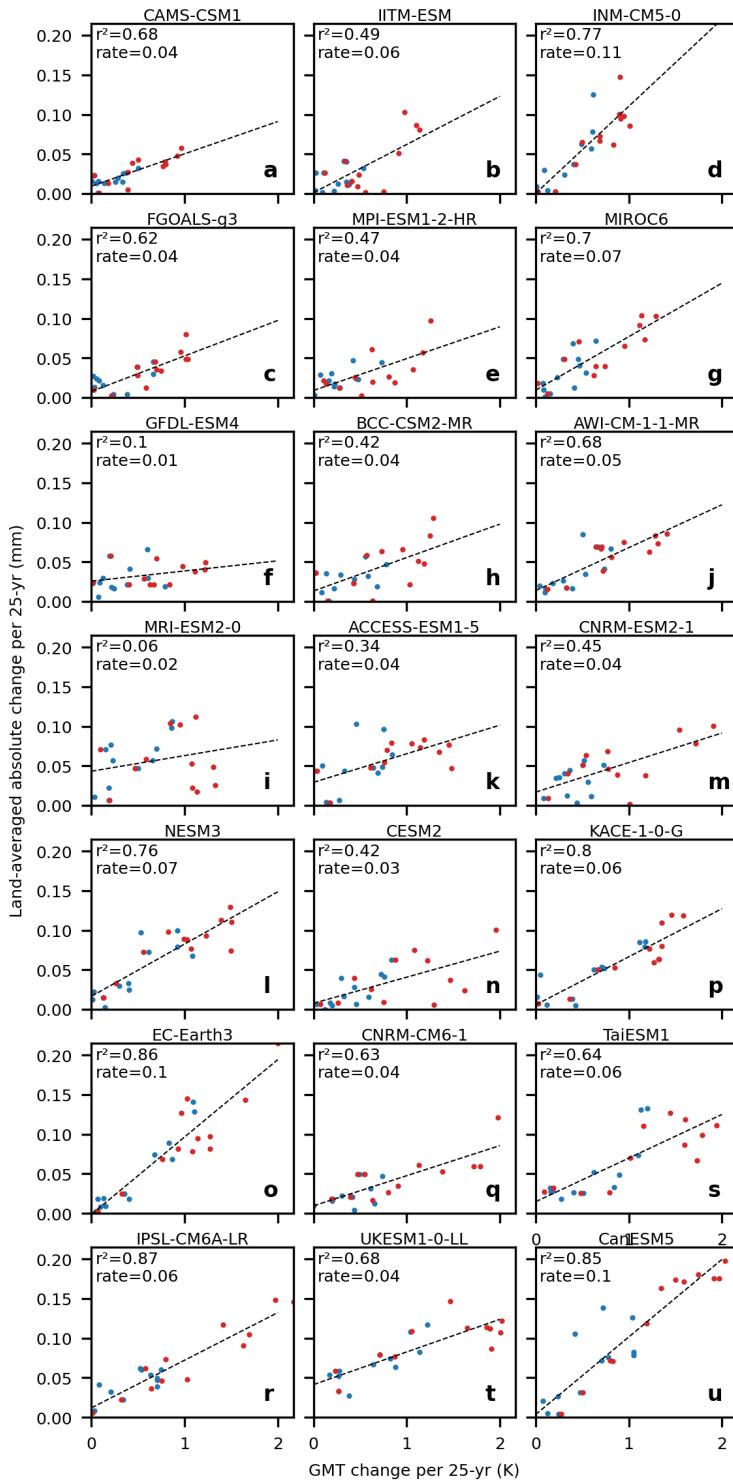


FIG. B6. As Fig. B2 but without having first applied LFCA.

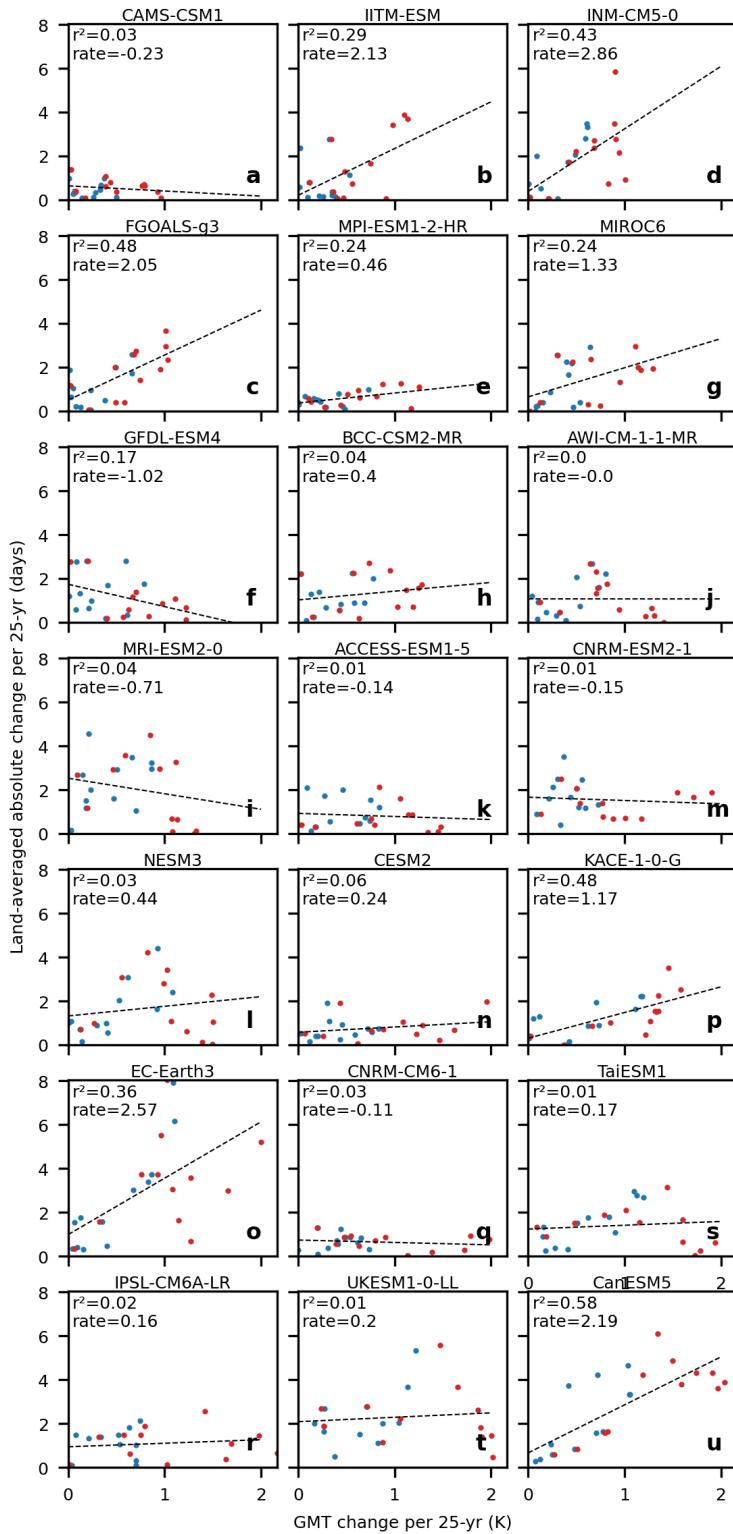


FIG. B7. As Fig. B3 but without having first applied LFCA.

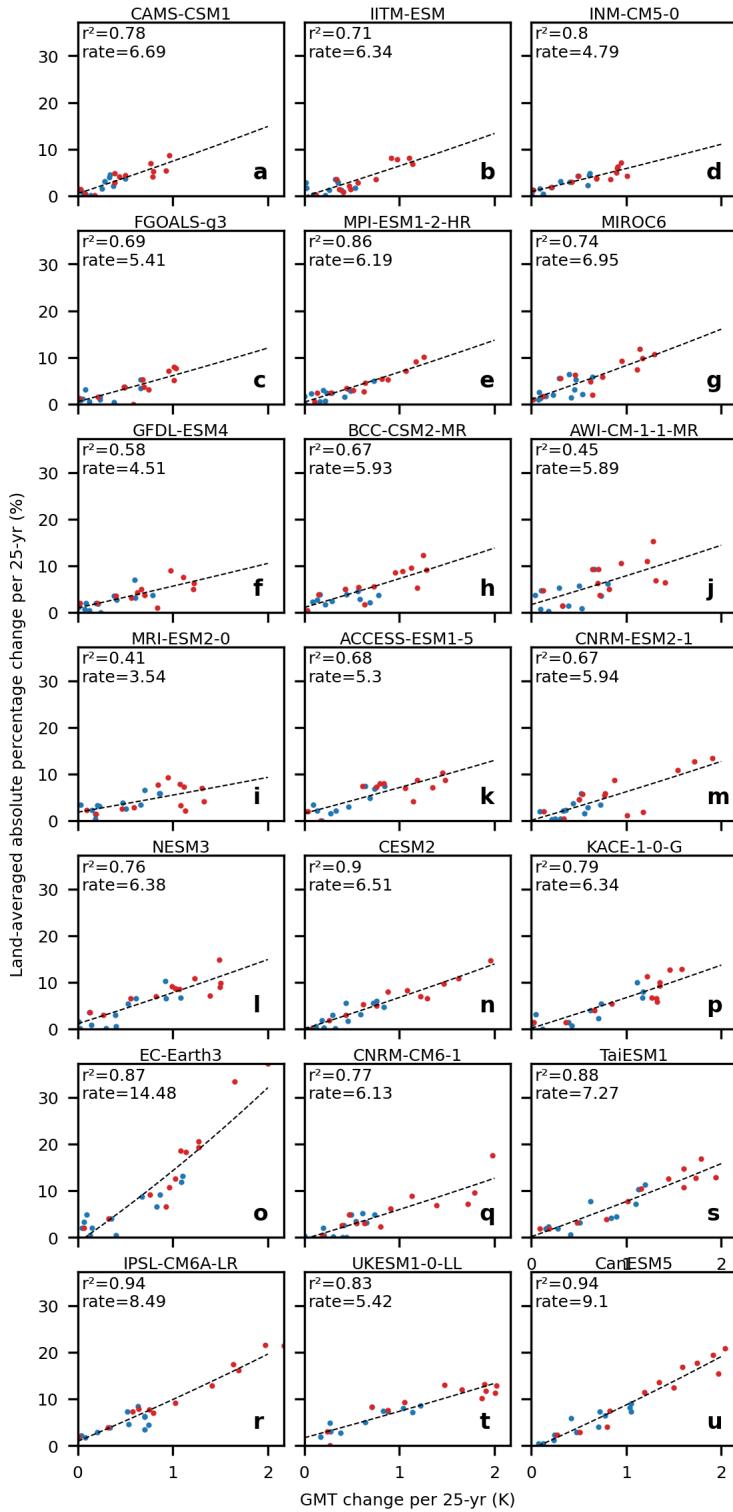


FIG. B8. As Fig. B4 but without having first applied LFCA.

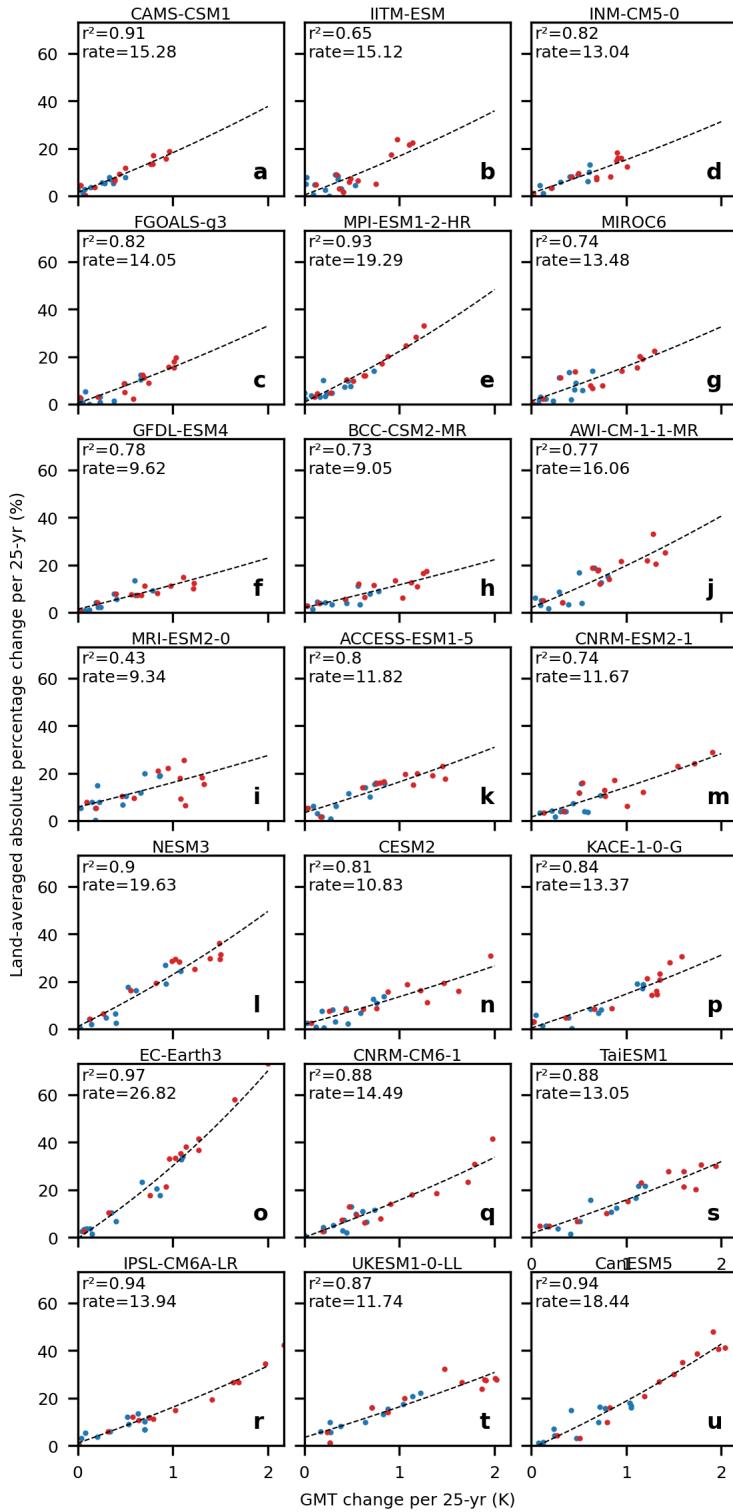
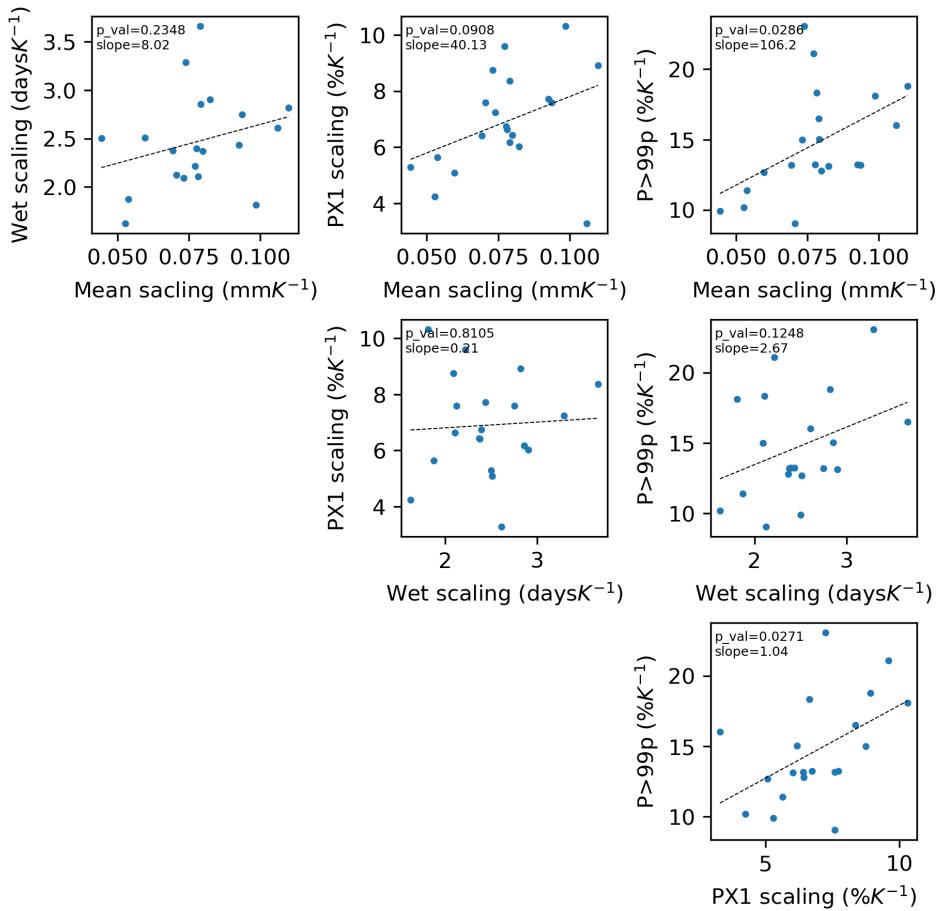


FIG. B9. As Fig. B5 but without having first applied LFCA.



432 FIG. B10. Co-variation between models of the scaling rates of different precipitation characteristics. "Mean",  
 433 "Wet", "PX1" and "P>99p" refer to the mean precipitation rate, the frequency of wet days, and the intensity and  
 434 frequency of daily extremes respectively.

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