

1 **Abrupt monsoon transitions as seen in paleo-records can be explained by**
2 **moisture-advection feedback**

3 Long version of Comment on “Near-linear response of mean monsoon strength to a
4 broad range of radiative forcings” by W.R. Boos and T. Storelvmo

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13 **Abrupt monsoon changes exist in paleo-records**

14 Paleo-climatic records show evidence of abrupt and strong monsoon shifts during the
15 last two glacial cycles (Burns et al. 2003; Wang 2005; Wang et al. 2008), the last
16 deglaciation (Stager et al. 2011) and the Holocene (Gupta et al. 2003; Hong et al. 2003;
17 Wang 2005; Berkelhammer et al. 2013; Dixit et al. 2014) in India, the Bay of Bengal,
18 and East Asia. While some of these shifts have been linked either to variations in solar
19 insolation or to climatic changes in other parts of the planet, they are often much more
20 abrupt and/or larger than expected for a linear response to external forcing, thus
21 suggesting that monsoon systems may be capable of non-linear transitions. Such
22 transitions were first reproduced in a conceptual model by (Zickfeld et al. 2005) and

23 later for the more specific case of the Wang et al. 2008 data by (Schewe et al. 2012).
24 Levermann et al. (2009) carved out the physical mechanism for such transition in a very
25 simple conceptual model stating in the abstract "Though details of monsoon circulations
26 are complicated, observations reveal a defining moisture-advection feedback that
27 dominates the seasonal heat balance and might act as an internal amplifier, leading to
28 abrupt changes in response to relatively weak external perturbations. Here we present a
29 minimal conceptual model capturing this positive feedback."

30 **Both conceptual models agree when operating in physically reasonable regime**

31 Boos & Storelvmo (2015) based their article on the statement that the introduction of
32 adiabatic cooling into the conceptual monsoon model of Levermann et al. (2009)
33 eliminates the abrupt transitions. That is not true as can be seen in their figure 1a. Boos
34 & Storelvmo obtain the same abrupt transition if the adiabatic cooling is not
35 compensating for the latent heat release. Thus their argument is based on the
36 assumption that most of the energy from latent heat release is consumed by adiabatic
37 cooling. While we are obviously aware of the existence of the physical process of
38 adiabatic cooling (and show below that it is implicitly accounted for in our model), it is
39 not a valid assumption that most of the latent heat release is consumed by this process.
40 To the contrary, the monsoon circulation over the continent is predominantly sustained
41 by the release of latent heat and subsequent warming of the atmospheric column over
42 land as stated in a number of classic studies as for example (Webster et al. 1998).
43 For that reason we deliberately addressed in our minimalistic model (and we clearly
44 declared this in the article) the simplest, but fundamentally important cases with

45 predominantly advective character of the low-atmosphere circulations in the main
46 monsoon regions. These situations are illustrated by Figure S2 from our article, where
47 we showed maps of the low-troposphere winds over these regions, with dominant
48 contribution from the advective component. It is further shown in our Figure 2 which
49 compares the latent heat release to other energy components for different regions.

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51 **Adiabatic cooling in the Levermann et al. (2009) model**

52 A very specific incorporation of adiabatic cooling into our conceptual model let Boos and
53 Storelvmo (2015) to their central result of a vanishing of the threshold in monsoon
54 rainfall. The specific representation they choose is based on an approximation of the
55 second horizontal derivative of the temperature by a linear function of its first horizontal
56 derivative (horizontal velocity), dividing the velocity scale by the horizontal length scale
57 (their equations (1)-(3) and (S1) and (S2)). This approximation is very crude. Here we
58 show that our model implicitly incorporates adiabatic cooling without eliminating the
59 possibility of abrupt monsoon transitions as seen in paleo-records:

60 Levermann et al. 2009 paper is based on the classical equations and conventional
61 assumptions. In that article we start with the equation for the specific entropy (see, e.g.,
62 (Lorenz 1967, page 13)) in z-coordinate:

$$63 \quad \frac{ds}{dt} = \frac{Q_m}{T} , \quad (1)$$

64 where $s = c_p \ln \theta$ is the specific entropy of the air, c_p and θ are the specific heat at
 65 constant pressure and the potential temperature of the air, t is time, Q_m is the net
 66 heating rate per unit mass, and T is kinetic temperature. Multiplying the left hand side of
 67 equation (1) by the air density ρ and using the continuity equation yields:

$$68 \quad \rho \frac{ds}{dt} = \frac{\partial \rho s}{\partial t} + \nabla \cdot (\rho s \vec{V}), \quad (2)$$

69 where $\partial/\partial t$ is the partial derivative with respect to time, ∇ is the three-dimensional
 70 gradient vector, \vec{V} is the three-dimensional vector of atmospheric velocity, and \cdot is a
 71 scalar multiplication sign. Integrating equation (2) with respect to z vertically from the
 72 earth's surface to the tropopause and horizontally over the monsoon land region,
 73 assuming quasi-stationarity of the process and imposing zero boundary conditions on
 74 the vertical velocity w at the surface and at the tropopause, z_{tr} , using equation (2) one
 75 obtains

$$76 \quad c_p \int_{\Sigma} \left(\int_0^{z_{tr}} \nabla_H \cdot \rho \theta \vec{V}_H dz \right) d\sigma = \int_{\Sigma} \left(\int_0^{z_{tr}} \frac{\theta}{T} Q_{V,P} dz \right) d\sigma + \int_{\Sigma} \left(\int_0^{z_{tr}} \frac{\theta}{T} Q_{V,R} dz \right) d\sigma, \quad (3)$$

77 where ∇_H is the horizontal gradient vector, \vec{V}_H is the vector of the horizontal velocity,
 78 Σ is the total area of the monsoon land region, while $Q_{V,P}$ and $Q_{V,R}$ are, respectively
 79 the net heating rate per unit volume due to the condensation and radiation. In our
 80 simple monsoon model we neglected the sensible heat flux at the land surface. The
 81 condensation heating rate is positive throughout the entire troposphere. The radiation
 82 heating rate is non-positive throughout the entire troposphere in the monsoon land

83 regions (McFarlane et al. 2007). The factor ϑ/T is positive in the troposphere. Thereby
84 one can bring this factor outside the integrals in the right side of equation (3),
85 representing it by constant parameters S_P , and S_R , respectively, in the first and
86 second terms in the right hand side of equation (3). We can denote S_P , and S_R as the
87 integral static stability parameters of the monsoon land system, associated with the
88 condensation and radiation processes. This way, the deviation of ϑ/T from 1 is the
89 indicator of the contribution from the vertical motions to the atmosphere heat balance: in
90 the adiabatic (i.e., with $T = \vartheta$) atmosphere the vertical motions could not contribute to
91 the heat balance. Equating condensation to precipitation rate over the monsoon land
92 region and prescribing as the parameter the ratio $\varepsilon = H/L$, where H and L are
93 respectively, the vertical extent of the lower branch of the monsoon inflow to the land
94 and the horizontal scale (distance between the coast line and the remote boundary of
95 the monsoon region, see Levermann et al. 2009), we get the equation whose general
96 structure is identical to Eq. (1) from that paper, namely

$$97 \quad LPS_P - \varepsilon c_p W \Delta T + RS_R = 0, \quad (4)$$

98 where L is the latent heat of condensation, P and R are the averaged over the entire
99 monsoon land region precipitation and radiation rates per unit square, and

$$100 \quad W = \alpha \Delta T, \quad (5)$$

101 where α is a constant parameter and $\Delta T = T_L - T_o > 0$ is atmospheric temperature
102 difference between land and ocean.

103 When deriving equation (4) we use a conventional representation of the potential
 104 temperature $\mathcal{G} \approx T + \gamma_A z$ within the troposphere, where γ_A is the constant adiabatic
 105 lapse rate, so that the horizontal derivatives of \mathcal{G} and T match up in that case.

106 A conservation law for the water vapor mass places a condition that an overall influx of
 107 the water vapor into the system should be equal to zero, for the steady states. This
 108 means, in our case, that in the absence of the land evaporation and under the condition
 109 that the vertical velocity is zeroed at the surface and at the tropopause, an overall
 110 (integrated over the entire side surface of the monsoon land region) income of water
 111 vapor at the lateral boundaries of the system should be balanced by the outcome of
 112 water vapor due to precipitation rate integrated over the entire lower surface of the
 113 monsoon land region. Going this way we get the equation for the atmospheric humidity
 114 that is identical to the equation (3) from Levermann et al. 2009:

$$115 \quad \varepsilon W \rho (q_o - q_L) - P = 0, \quad (6)$$

116 where q_o and q_L are the specific humidity over ocean and land, respectively.

117 We further represent P as follows (see Levermann et al. 2009):

$$118 \quad P = \beta q_L, \quad (7)$$

119 where β is constant parameter. Finally, combining equations (4) - (7) one can get

$$120 \quad W^3 + \frac{\beta}{\varepsilon \rho} W^2 - \frac{\alpha}{\varepsilon c_p} (LS_p \beta q_o + RS_R) W - \frac{\alpha \beta}{\varepsilon^2 \rho c_p} RS_R = 0, \quad (8)$$

121 The general structure of this equation is identical to that of the governing equation in
122 Levermann et al. 2009.

123 As a consequence, the threshold behavior is not eliminated by adiabatic cooling unless
124 it consumes practically all of the energy of the latent heat release.

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